

PAGE 9 Formulae for PHYS101 Final Examination (April 2007)

Fluids: $P = P_0 + \rho gh$, $\rho vA = \text{constant}$ or $A_1v_1 = A_2v_2$ $F_B = \rho_F V_F g$

$$P + \frac{1}{2} \rho v^2 + \rho gh = \text{constant} \quad Q = \pi R^4 (P_1 - P_2) / (8\eta L) \quad M_{\text{apparent}} = V(\rho - \rho_F)$$

Harmonic Motion: $F = -kx$ (k = spring constant) $\text{PE} = \frac{1}{2} k x^2$ $\text{KE} = \frac{1}{2} mv^2$
 $x(t) = A \cos(\omega t + \phi)$ $v(t) = -A\omega \sin(\omega t + \phi)$ $a(t) = -A\omega^2 \cos(\omega t + \phi) = -\omega^2 x(t)$

$$\omega = \sqrt{\frac{g}{l}}$$
 (Pendulum); $E = \frac{1}{2} k A^2 = \frac{1}{2} m v_{\text{max}}^2$; $A(t) = A(0) \exp(-bt/2m)$; $\omega = (\frac{k}{m})^{1/2}$

Travelling Waves: $k = \frac{2\pi}{\lambda}$ $\omega = \frac{2\pi}{T} = 2\pi f$ $v = \lambda f$ $v = \sqrt{\frac{F_T}{\mu}}$

Harmonic Waves: $y(x, t) = A \sin(kx + \omega t + \phi)$ or $y(x, t) = A \sin(kx - \omega t + \phi)$

$$v_y(x, t) = \omega A \cos(kx + \omega t + \phi) \text{ or } v_y(x, t) = -\omega A \cos(kx - \omega t + \phi)$$

Standing waves: $y = 2A \sin kx \cos \omega t$

Sound: $\text{Intensity} = \text{Power/Area}$

$$\beta(\text{dB}) = 10 \log_{10} \left(\frac{I}{I_0} \right) \quad I_0 = 10^{-12} \frac{W}{m^2} \quad \text{spherical wave} \quad I = \frac{P}{4\pi r^2} \quad f' = f \left(\frac{v \pm v_o}{v \mp v_s} \right)$$

Interference : Index of refraction : $n = \frac{c}{v}$ $\lambda_n = \frac{\lambda}{n}$

Phase difference upon reflection = π (hard, $n_2 > n_1$) or = 0 (soft, $n_2 < n_1$)

$$\text{Optical path length} = nd \quad \text{phase difference} = \frac{2\pi}{\lambda} (\text{path difference})$$

N-slit interference: $d \sin \theta = m\lambda$ (constructive),

Diffraction: First single-slit diffraction minimum: $a \sin \theta = \lambda$ circular aperture: $\theta_{\min} = 1.22 \frac{\lambda}{D}$

Heat: $L = L_0(1 + \alpha(T - T_0))$ $Q = mc\Delta T$ $Q = mL$

$$dQ/dt = k A \Delta T / L \quad dQ/dt = e\sigma AT^4 \quad \sigma = 5.67 \times 10^{-8} \text{ W/m}^2\text{K}^4 \quad 0^\circ\text{C} = 273 \text{ K}$$

$$L_{\text{water-fusion}} = 3.33 \times 10^5 \text{ J/kg or 80.0 cals/gram}; \quad L_{\text{water-vap.}} = 22.6 \times 10^5 \text{ J/kg or 539 cals/gram};$$

$$c_{\text{ice}} = 2100 \text{ J/kg.}^\circ\text{C or 0.5 cal/gram}^\circ\text{C}, \quad c_{\text{water}} = 4186 \text{ J/kg.}^\circ\text{C or 1.0 cal/gram}^\circ\text{C}$$

$$c_{\text{steam}} = 2010 \text{ J/kg.}^\circ\text{C or 0.48 cal/gram}^\circ\text{C}$$

Constants: $P_{\text{atmosphere}} = 1.013 \times 10^5 \text{ Pa}$, ρ (fresh water) = 1000 kg/m^3 , ρ (He) = 0.18 kg/m^3

$$\rho(\text{air}) = 1.29 \text{ kg/m}^3, \quad \rho(\text{ice}) = 917 \text{ kg/m}^3 \quad \eta_{\text{water}} = 1.0 \times 10^{-3} \text{ Pa.sec.}$$

Velocity of sound in air = 343 m/s , $1 \text{ cal.} = 4.186 \text{ J}$, $g = 9.81 \text{ m/s}^2$, Vel. of light, $c = 3 \times 10^8 \text{ m/s}$