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Part (t) | dt, e i what | H'ba (t) | dt, e

TRANSITION PROBABILITIES: H=Ha+HH) Initial state at t=to: (4a) Turns on at time to Probability of measuring particle in state (Vb) at time t $P_{a\rightarrow b}(t) = \frac{1}{t^2} \left| \int_{t_0}^{t} dt, e^{i\omega_{ba}t}, H_{ba}(t_i) \right|^2$ $= \frac{1}{t^2} \left| \int_{t_0}^{t} dt, e^{i\omega_{ba}t}, H_{ba}(t_i) \right|^2$

A system of two spins has a Hamiltonian $H = \frac{\Omega}{\hbar}J^2$ where $\vec{J} = \vec{S}_1 + \vec{S}_2$. At t = 0, the system is in the state

$$|J=1, M=0\rangle = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle)$$
 (4)

Starting at t = 0, a time-dependent perturbation

$$H_1 = Ae^{-bt}S_2^z (5)$$

is added to the Hamiltonian, where $S_2^z = 1 \otimes S^z$ is the z-component of the spin for the second particle.

a) In the approximation of first order time-dependent perturbation theory, what is the probability that the system will have made a transition to the J=0 state

$$|J=0, M=0\rangle = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) .$$
 (6)

at time $t = \infty$? (4 points)

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Part (4) =
$$\frac{1}{t^2} \left| \int_{t_0}^{t} dt$$
, $e^{i\omega_{ba}t}$, $H'_{ba}(t_1) \right|^2$

(2) -a and o and t

(3) o and t

(5) -a and b

01: What are to and t?

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Q3: what is HLa(t)?

$$|J=0,M=0\rangle = \frac{1}{\sqrt{2}} (|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle) . \tag{6}$$

at time $t = \infty$? (4 points)

$$H = \frac{p^2}{2m} + \frac{1}{2}k(t)x^2 \; ,$$

where

$$k(t) = m\omega_0^2 + \frac{K}{1 + \left(\frac{t}{\tau_0}\right)^2}.$$

a) At $t=-\infty$, the system starts in the ground state of the Hamiltonian at that time. For small values of the parameter K, estimate the probability that the system will have made a transition to some other state, by $time t=\infty$.

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$$\frac{p^2}{2m} + \frac{1}{2}m\omega_0^2 X^2$$

$$\frac{p^2}{2m} + \frac{1}{2}(m\omega_0^2 + k) \times^2$$

$$\frac{P^2}{2m} + \frac{1}{2} \left(m\omega_0^2 + \frac{K}{1 + (t_0)^2} \right) \times^2$$

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OZ: What is H(t)?

(1)
$$\frac{1}{2} m \omega_o^2 x^2 + \frac{1}{2} \frac{K}{1 + (t_{\tau_o})^2} x^2$$
(2) $\frac{1}{2} \frac{K}{1 + (t_{\tau_o})^2} x^2$

$$\frac{1}{2m} + \frac{1}{2} m \omega_0^2 x^2$$

$$(4) - \frac{t \times^2 K}{(1 + (\frac{t}{\tau_0})^2)^2}$$

Park (4) =

where

a) At $t = -\infty$, the system starts in the ground state of the Hamiltonian at that time. For small values of the parameter K, estimate the probability that the system will have made a transition to some other state.

Q3: The system starts in the state 10). To which other states can we make a transition (in the approximation of 1st order perturbation theory?)

Hint: What is Hba?

(DISCUSSION)

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Q4: What is who?

Problem 3

A particle of mass m is in the ground state of an infinite square well potential of width a. Starting at t = 0, the potential in the left half of the well increases at a constant rate from 0 to V in time T and then decreases back to zero at a constant rate in time T. If V is small, what is the probability that the particle will be found in the first excited state of the well at time 2T? Hint: the formula sheet should help.

$$P_{a\rightarrow b} = \frac{1}{t^2} \left| \int_{t_0}^{t} dt, \ e^{i\omega_{ba}t} H'_{ba}(t) \right|^2$$

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$$P_{a\rightarrow b} = \frac{1}{t^2} \left| \begin{cases} t \\ dt, e \end{cases} \right|^2 H_{ba}(t) \left| \begin{cases} t \\ t \end{cases} \right|^2$$

* Useful formulae:
$$\sqrt{n(x)} = \sqrt{\frac{2}{a}} \cdot \sin\left(\frac{n\pi x}{a}\right)$$
 (Discussion)

Videos ("reading" for Thesday)

① Parab for a sinusoidal time dependence
② Types of atomic transitions
③ H for a charged particle in an EM field

(4) HH for an atom/molecule in an EM wave