

What equation in classical physics does

$$i \frac{\hbar}{2\pi} \frac{\partial \psi}{\partial t} = - \left(\frac{\hbar}{2\pi} \right)^2 \frac{1}{2m} \frac{\partial^2 \psi}{\partial x^2}$$

replace?

A) Maxwell's equations (for the propagation of electromagnetic waves)

B) The classical wave equation:

$$\frac{\partial^2 h}{\partial t^2} = v^2 \frac{\partial^2 h}{\partial x^2}$$

C) Newton's Second Law: $\mathbf{F} = m \mathbf{a}$

D) Newton's First Law: $m \mathbf{a} = 0$ in the absence of forces

Answer: D $m \mathbf{a} = 0$

classical

quantum

description:

$$x(t)$$

$$\psi(x, t)$$

free particle
equation of motion:

$$m \ddot{x} = 0$$

$$i \frac{\hbar}{2\pi} \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{(2\pi)^2 2m} \frac{\partial^2 \psi}{\partial x^2}$$

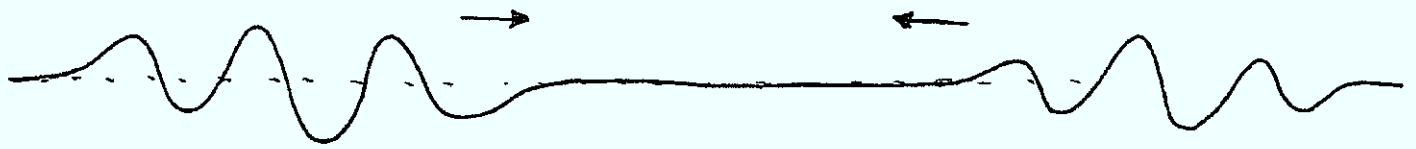
free particle solutions:

$$x = x_0 + vt$$

$$\psi(x, t) = \frac{1}{\sqrt{h}} \int dp \chi(p) e^{i \frac{2\pi}{h} (px - \frac{p^2}{2m} t)}$$

TODAY: what replaces: $m \ddot{x} = F = -V'(x)$?

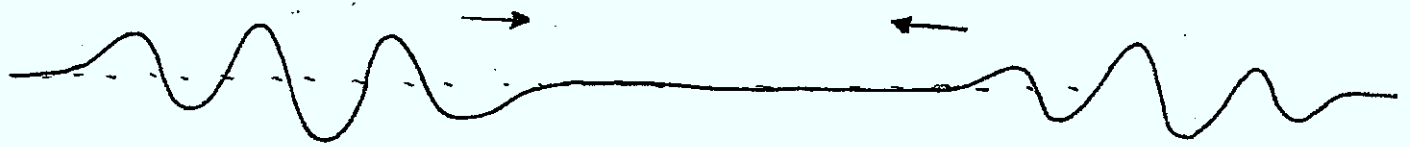
$\text{Re}(\psi(x))$



The wavefunction for an electron involves two wavepackets traveling in opposite directions. When they meet, the wavepackets will

- A) Pass right through each other
- B) Repel each other and reverse directions
- C) Attract each other and form a bound state.

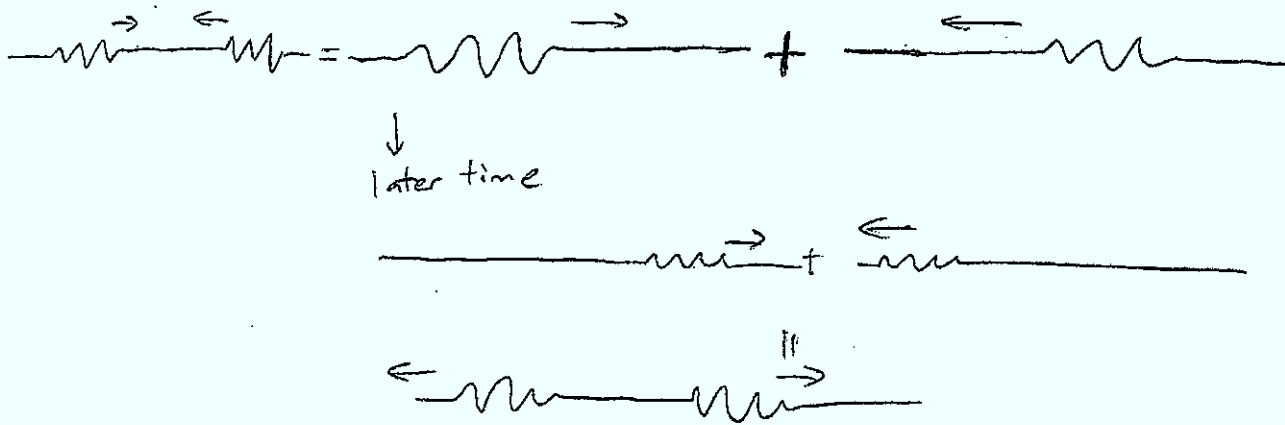
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Schrodinger eqn \rightarrow sum of any 2 solns is a solution.



An electron with momentum p travels in a region where it has a constant positive potential energy V . Compared to an electron with the same momentum p in a region with zero potential energy, we expect that this electron's wavefunction will have

- A) a larger wavelength
- B) a smaller wavelength
- C) a larger frequency
- D) a smaller frequency
- E) both B and C

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B) a smaller wavelength

C) a larger frequency $frequency = energy/h = (p^2/(2m) + V)/h$

D) a smaller frequency

E) both B and C

Which of the following should be true of an energy eigenstate?

- A) The time dependence of the wavefunction should be a simple oscillation of the phase with a definite frequency.
- B) There should be zero uncertainty in the quantity $p^2/(2m) + V(x)$.
- C) The probability density should be independent of time.
- D) All of the above.

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D) All of the above.

$$\text{energy} = h \times \text{frequency}$$

\therefore definite energy, definite freq

$$\psi(x,t) = \psi_E(x) e^{-i\frac{2\pi}{h}Et}$$

$$\text{also: } |\psi(x,t)|^2 = |\psi_E(x)|^2 \text{ indep. of time}$$

also: definite energy

\Rightarrow zero uncertainty in

$$\frac{p^2}{2m} + V(x)$$