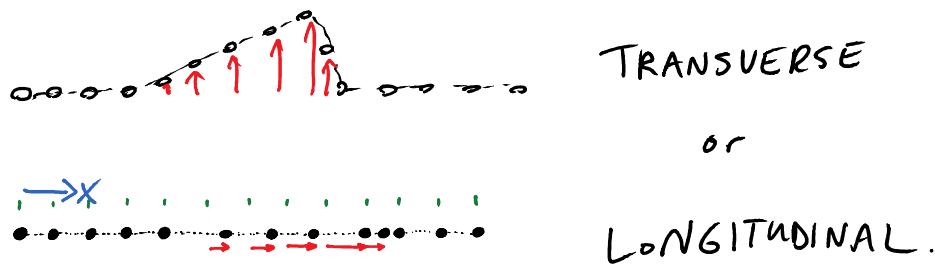


# LAST TIME: Waves



Mathematical description:

$D(x, t)$  → tells us how much point  $x$  is displaced at time  $t$

e.g.  $F(x) = D(x, 0)$  : shape of wave pulse at time  $t=0$

C1

Right-moving pulse:  $D(x, t) = F(x - vt)$

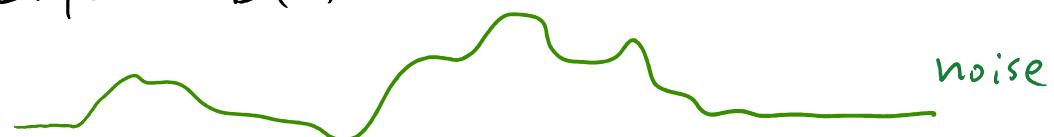
Left-moving pulse:  $D(x, t) = F(x + vt)$

C2 SOUND IS A LONGITUDINAL WAVE

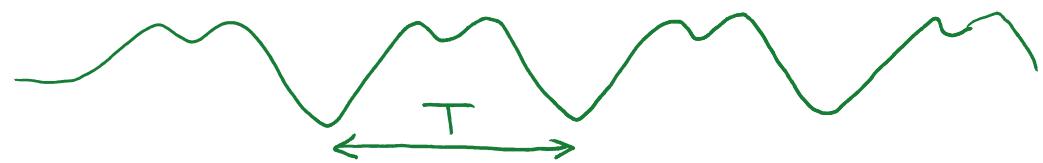
TODAY Sound & Music:

Q1: What distinguishes musical notes from other sounds?

A: The shape of  $D(t)$



Note:

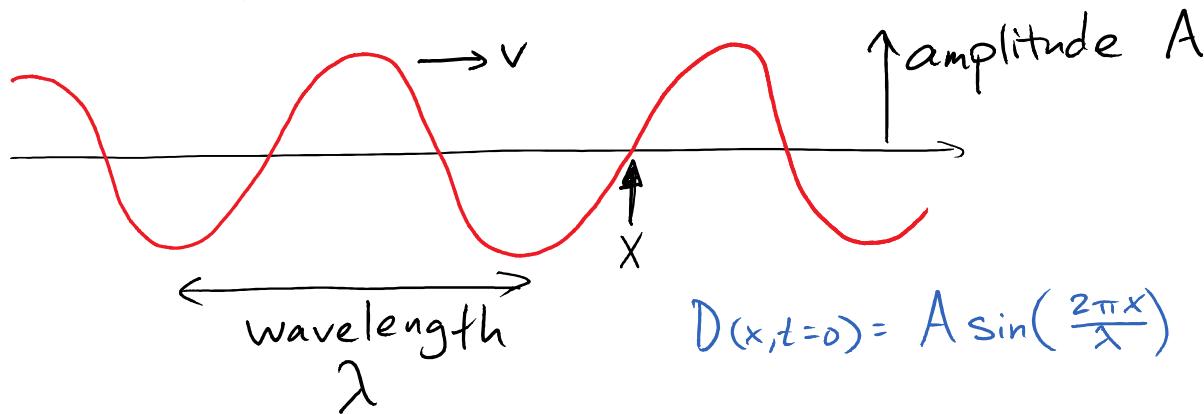


Note:  $D$  repeats w. definite period  $T$

frequency is  $\frac{1}{T}$

Important example: sinusoidal waves = "PURE TONE"

snapshot:



At point X: time dependence is also sinusoidal

$$D(x,t) = A \sin\left(\frac{2\pi}{\lambda}(x - vt)\right)$$

(right moving)

KEY RELATION:

$$f = \frac{v}{\lambda}$$

shorter wavelength: peaks pass X more frequently  
∴ higher frequency

$$\text{lingo: } \frac{2\pi}{\lambda} = k \quad \begin{matrix} \text{WAVE} \\ \text{NUMBER} \end{matrix}$$

$$2\pi f = \omega \quad \begin{matrix} \text{ANGULAR} \\ \text{FREQUENCY} \end{matrix}$$

$$D(x,t) = A \sin(kx - \omega t)$$

## Back to music:

What distinguishes "high" and "low" sounds, or different notes?

High = larger frequency    Low = smaller frequency

Why do different instruments sound different?

Any wave w. frequency  $f$  = sum of sinusoidal waves w. frequencies  $f, 2f, 3f, 4f \dots$  w. different amplitudes. (These are HARMONICS of a note)  
Different instruments playing same note → different combinations of harmonics

Why do some notes sound good together?

Notes sound good together if ratio of frequencies is a simple fraction

e.g. 1:2 (octave)

2:3 (fifth)

3:4 (fourth)

What distinguishes "high" and "low" sounds, or different notes?

Why do different instruments sound different?

What determines the sound of an instrument?

How can the same tube/string/etc... make different sounds?

Why do some notes sound good together?