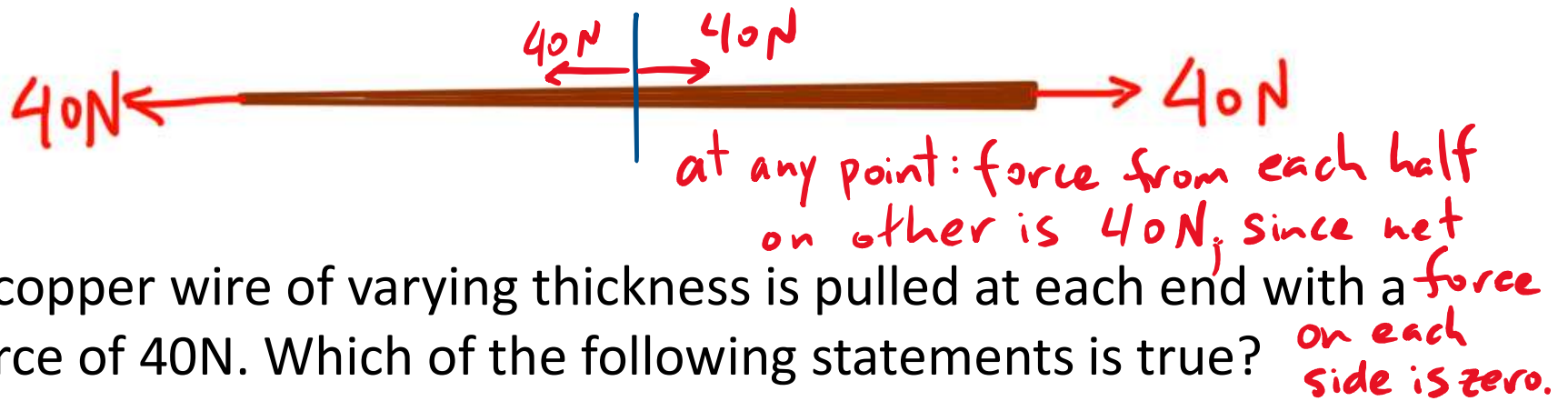




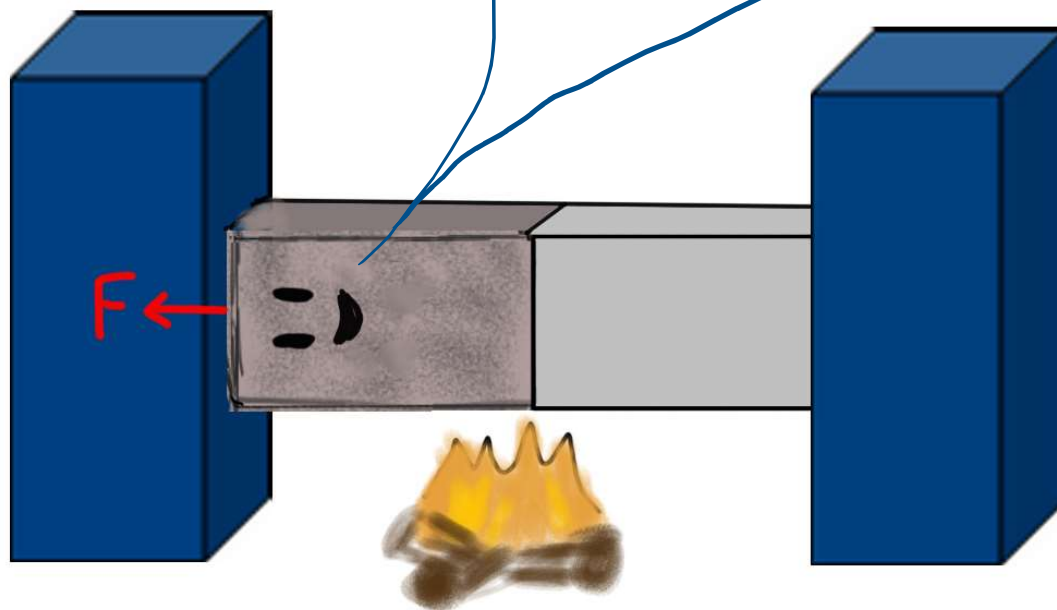
A copper wire of varying thickness is pulled at each end with a force of 40N. Which of the following statements is true?

- A) The tension is a constant 80N all along the wire, and the stress is also constant along the wire.
- B) The tension is a constant 40N all along the wire, and the stress is also constant along the wire.
- C) The stress is constant throughout the wire but the tension varies.
- D) The tension is a constant 80N all along the wire, but the stress varies along the wire.
- E) The tension is a constant 40N all along the wire, but the stress varies along the wire.

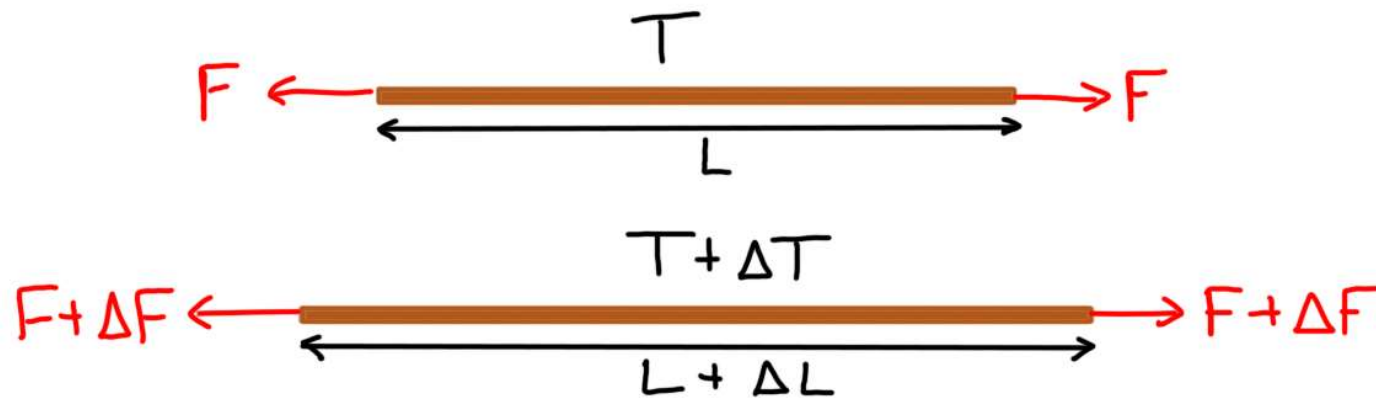


- A) The tension is a constant 80N all along the wire, and the stress is also constant along the wire.
- B) The tension is a constant 40N all along the wire, and the stress is also constant along the wire.  $\text{stress} = F/A$
- C) The stress is constant throughout the wire but the tension varies. *varies since A*
- D) The tension is a constant 80N all along the wire, but the stress varies along the wire. *varies*
- E) The tension is a constant 40N all along the wire, but the stress varies along the wire.

Last time  
in Physics  
157...



Expansion from changes in temperature and stress :



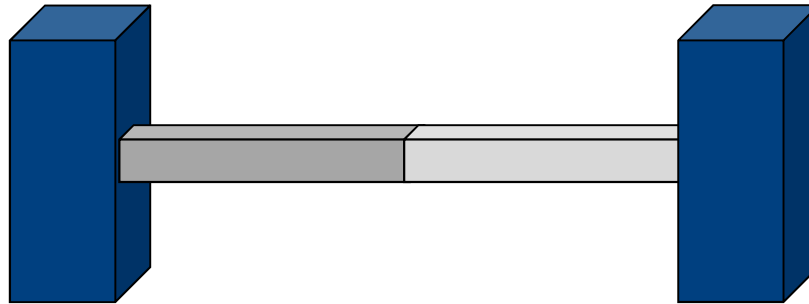
$$\Delta L = (\Delta L)_T + (\Delta L)_F$$

$$\Delta L = \alpha L \Delta T + \frac{L}{Y} \cdot \frac{\Delta F}{A}$$

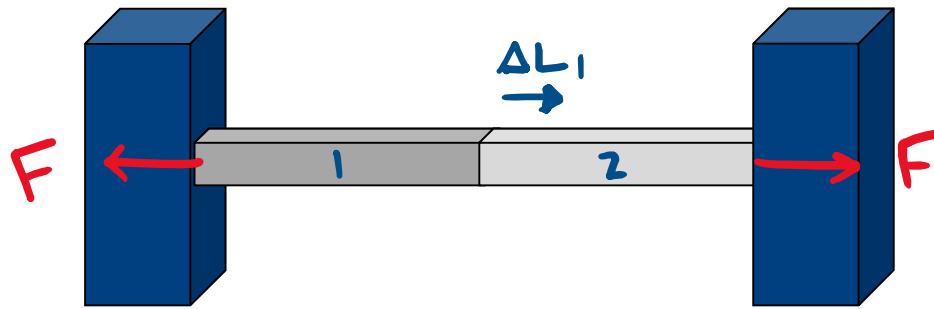
# Stressed Rods

A compound bar consisting of a copper rod with a length of 1 m and cross-section area of  $2.00 \text{ cm}^2$  placed end to end with a steel rod with length 1 m and cross-section area  $2.00 \text{ cm}^2$ . The compound rod is placed between two rigid walls. Initially there is no stress in the bars at room temperature  $20^\circ \text{ C}$ .

Find the force on each wall at  $40^\circ \text{ C}$ .



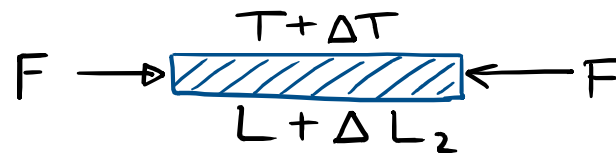
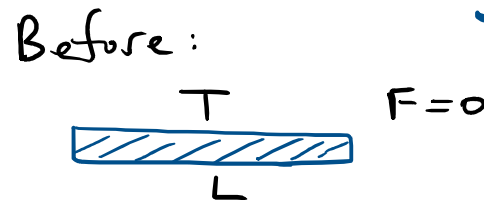
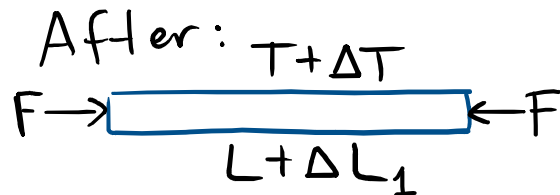
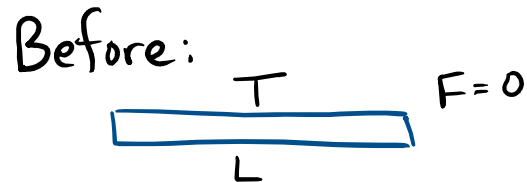
$$\alpha_{\text{steel}} = 12 \times 10^{-6} \text{ K}^{-1}, \alpha_{\text{copper}} = 17 \times 10^{-6} \text{ K}^{-1},$$
$$Y_{\text{steel}} = 200 \times 10^9 \text{ N m}^{-2}, Y_{\text{copper}} = 110 \times 10^9 \text{ N m}^{-2}$$



rigid ends:

$$\Delta L_1 + \Delta L_2 = 0$$

Newton's Laws:  
all forces have  
magnitude  $F$



Length change from  
 $\Delta T$  and  $\Delta F$ :

$$\Delta L_1 = \alpha_1 L \Delta T - \frac{F}{A} \cdot \frac{L}{Y_1}$$

$$\Delta L_2 = \alpha_2 L \Delta T - \frac{F}{A} \cdot \frac{L}{Y_2}$$

$$\Delta L_1 + \Delta L_2 = 0$$

①

$$\Delta L_1 = \alpha_1 L \Delta T - \frac{F}{A} \cdot \frac{L}{Y_1}$$

②

$$\Delta L_2 = \alpha_2 L \Delta T - \frac{F}{A} \cdot \frac{L}{Y_2}$$

③

Plug ② and ③ into ①:

$$\alpha_1 L \Delta T + \alpha_2 L \Delta T - \frac{F}{A} \frac{L}{Y_1} - \frac{F}{A} \frac{L}{Y_2} = 0$$

Isolate terms with F:

$$\frac{F \cdot L}{A} \left( \frac{1}{Y_1} + \frac{1}{Y_2} \right) = (\alpha_1 + \alpha_2) L \Delta T$$

Solve:

$$F = \frac{(\alpha_1 + \alpha_2) \Delta T}{\left( \frac{1}{Y_1} + \frac{1}{Y_2} \right)} \cdot A = 8.2 \times 10^3 \text{ N}$$

If you find it annoying to use your calculator...



Type some Sage code below and press Evaluate.

```
1 alpha1 = 12*10^(-6)
2 alpha2 = 17*10^(-6)
3 Y1 = 200*10^9
4 Y2 = 110*10^9
5 DT = 20
6 A = 2.0*10^(-4)
7 A*DT*(alpha1 + alpha2)/(1/Y1 + 1/Y2)
8
```

← type in your constants

← type in your formula

Evaluate

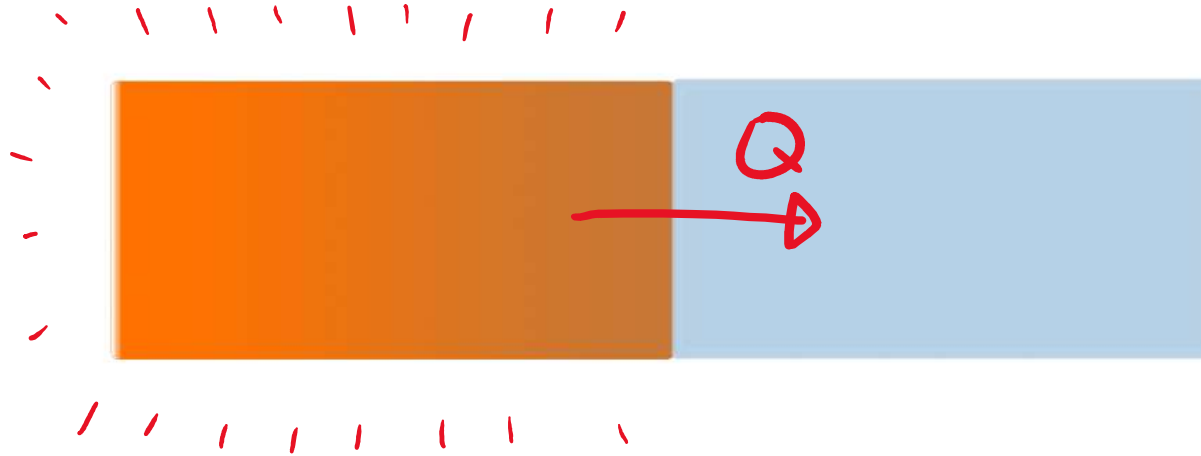
← click

8232.25806451613

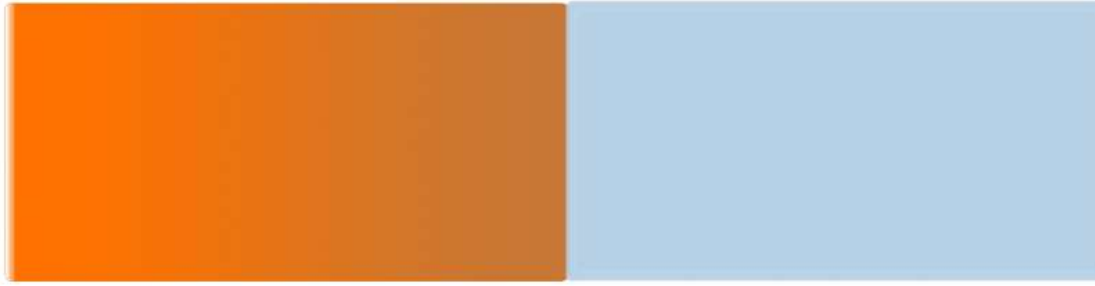
← answer



# HEAT:

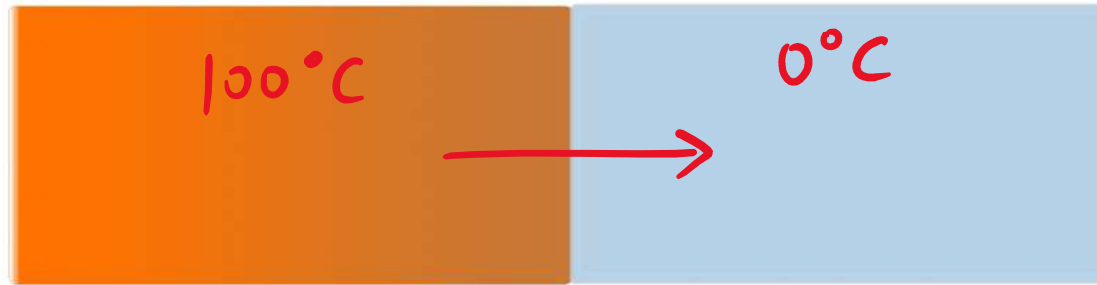


$Q$  = heat : amount of energy transferred  
(Joules) due to temperature differences



**Clicker:** two objects with the same mass are put in thermal contact but insulated from their environment. If the initial temperatures are  $100^{\circ}\text{C}$  and  $0^{\circ}\text{C}$ , the final equilibrium temperature will be

- A)  $50^{\circ}\text{C}$
- B) Somewhere between  $0^{\circ}\text{C}$  and  $100^{\circ}\text{C}$  but not necessarily  $50^{\circ}\text{C}$
- C) Not necessarily between  $0^{\circ}\text{C}$  and  $100^{\circ}\text{C}$



**Clicker:** two objects with the same mass are put in thermal contact but insulated from their environment. If the initial temperatures are  $100^{\circ}\text{C}$  and  $0^{\circ}\text{C}$ , the final equilibrium temperature will be

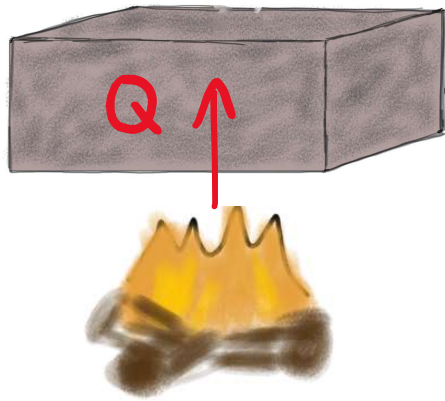
A)  $50^{\circ}\text{C}$

B) Somewhere between  $0^{\circ}\text{C}$  and  $100^{\circ}\text{C}$  but not necessarily  $50^{\circ}\text{C}$

C) Not necessarily between  $0^{\circ}\text{C}$  and  $100^{\circ}\text{C}$

- Heat flows from the hotter object to the cooler
- Temperature of the hot object decreases & the cold object increases, until they are the same temperature, between  $0^{\circ}$  and  $100^{\circ}$ .
- Not necessarily  $50^{\circ}$  since some materials require more energy for a given temperature change

Heat required to raise the temperature of a material determined by its SPECIFIC HEAT  $c$ :



$$Q = m c \Delta T$$

heat added

mass

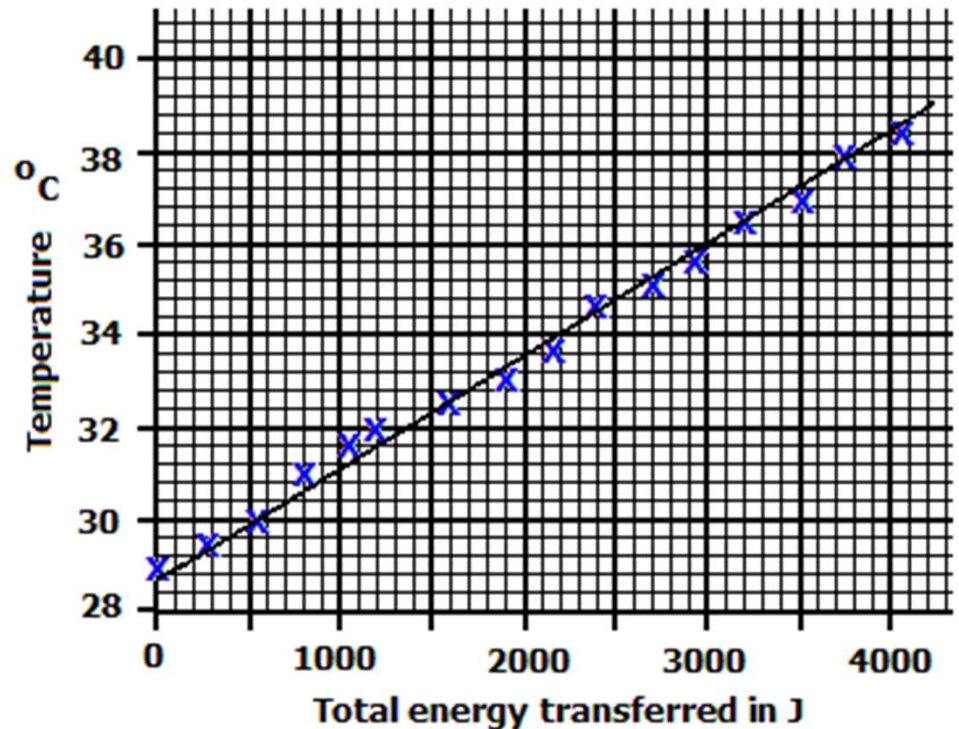
change in temperature

$c$  in  $\frac{\text{J}}{\text{kg} \cdot \text{K}}$  : energy required to heat 1 kg of material by 1 K

Heat is added to two kilograms of a liquid, and data for the temperature vs energy transfer is shown.

If we took data for another liquid with the same mass but a larger specific heat, the slope of this graph would be

- A) Larger
- B) Smaller
- C) The same
- D) Any of the above are possible.



$$Q = mc \Delta T$$

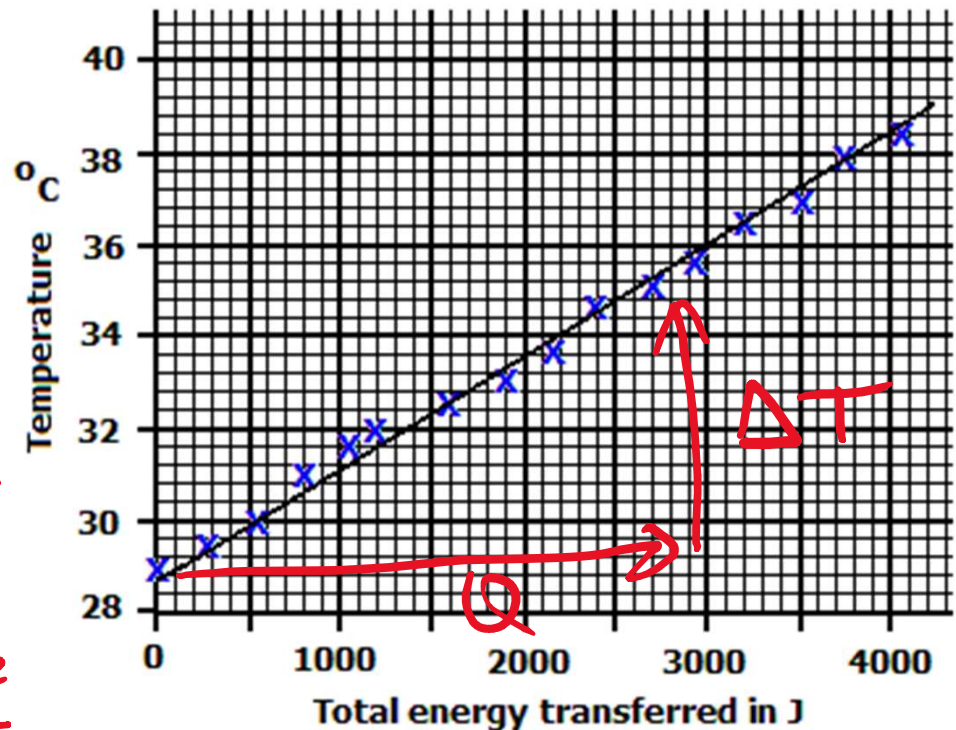
**EXTRA:** what is the specific heat of the original liquid?

Heat is added to two kilograms of a liquid, and data for the temperature vs energy transfer is shown.

If we took data for another liquid with the same mass but a larger specific heat, the slope of this graph would be

- A) Larger
- B) Smaller**
- C) The same
- D) Any of the above are possible.

Smaller  $\Delta T$   
for same  $Q$   
 $\therefore$  smaller  
rise  
run

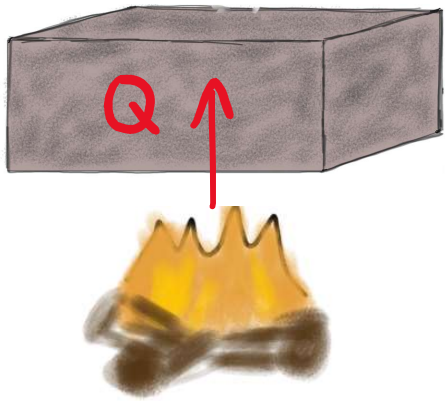


**EXTRA:** what is the specific heat of the original liquid?

$$c \approx \frac{3000}{7.2} \approx 200 \text{ J/kgK}$$

$$Q = mc\Delta T$$

Heat required to raise the temperature of a material determined by its SPECIFIC HEAT  $c$ :



$$Q = m c \Delta T$$

Annotations: A green arrow points from the word "mass" to the variable  $m$ . Another green arrow points from the word "SPECIFIC HEAT" (from the text above) to the variable  $c$ .

OR:

$$Q = n C \Delta T$$

Annotations: A green arrow points from the text "# moles" to the variable  $n$ . Another green arrow points from the text "MOLAR SPECIFIC HEAT" (from the text below) to the variable  $C$ .

MOLAR SPECIFIC HEAT  
= MOLAR HEAT CAPACITY

$$c \text{ in } \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

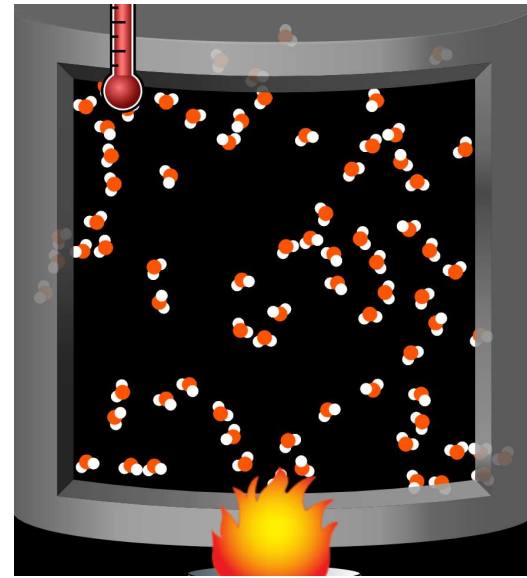
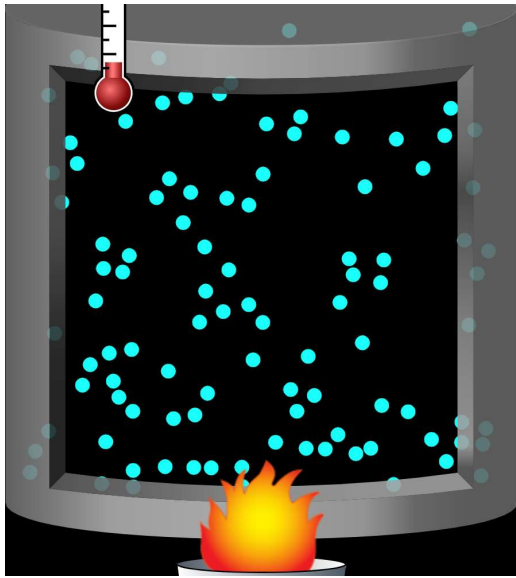
: energy required to heat 1 kg of material by 1K

$$C \text{ in } \frac{\text{J}}{\text{mol} \cdot \text{K}}$$

: energy required to heat 1 mole of material by 1K

# Why is heat capacity higher for some materials?

will see: temperature proportional to average kinetic energy of molecules



for more complicated materials, part of added energy added goes to rotations/vibrations etc..., so it takes more  $Q$  to increase the kinetic energy.





**Exercise:** two objects with the same mass are put in thermal contact but insulated from their environment. If the initial temperatures are  $100^{\circ}\text{C}$  and  $0^{\circ}\text{C}$ , and the specific heats are  $c_1 = 300 \text{ J/kg}\cdot\text{K}$  and  $c_2 = 900 \text{ J/kg}\cdot\text{K}$ , calculate the final equilibrium temperature.

*Hint: isolate the parts and think of what is happening to each part separately. Draw a picture and label it.*

**Click A if you are finished, B if you are totally stuck.**

$$Q = mc\Delta T$$