

Clicker question: In the picture below, box 2 is twice the height as box 1, with twice the number of molecules, moving at the same average speed. Compared to the pressure on the left wall of box 1, the pressure on the left wall in box 2 will be

A) the same.

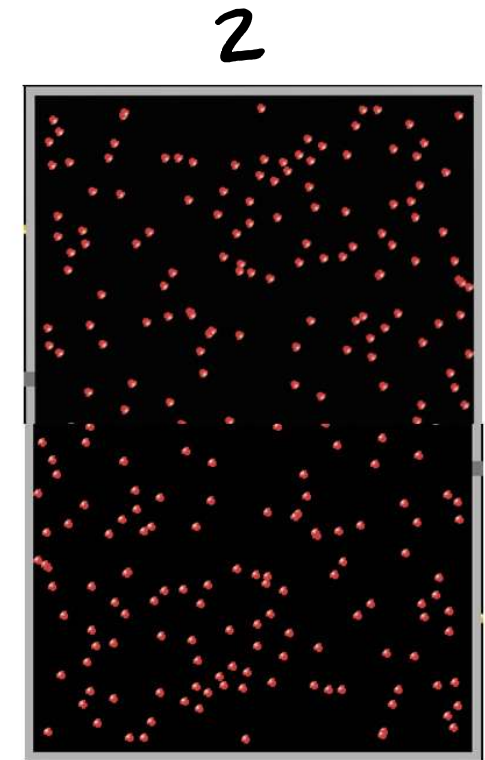
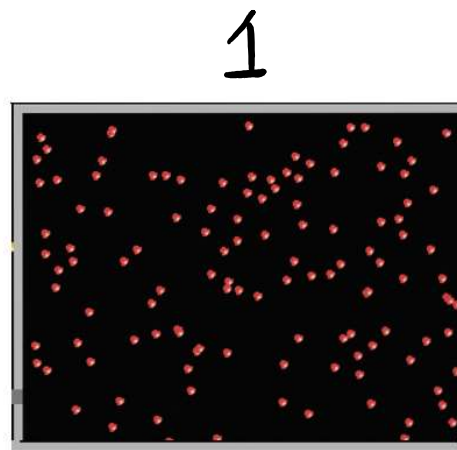
B) half.

C) double.

D) None of the above.

EXTRA: if we double the average speed of the molecules, give

TWO reasons why pressure would increase.



$$P = \frac{F}{A}$$

Clicker question: In the picture below, box 2 is twice the height as box 1, with twice the number of molecules, moving at the same average speed. Compared to the pressure on the left wall of box 1, the pressure on the left wall in box 2 will be

A) the same.

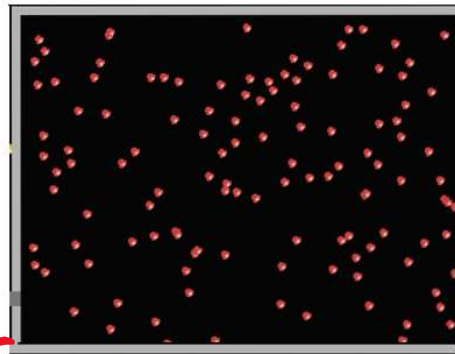
B) half.

C) double.

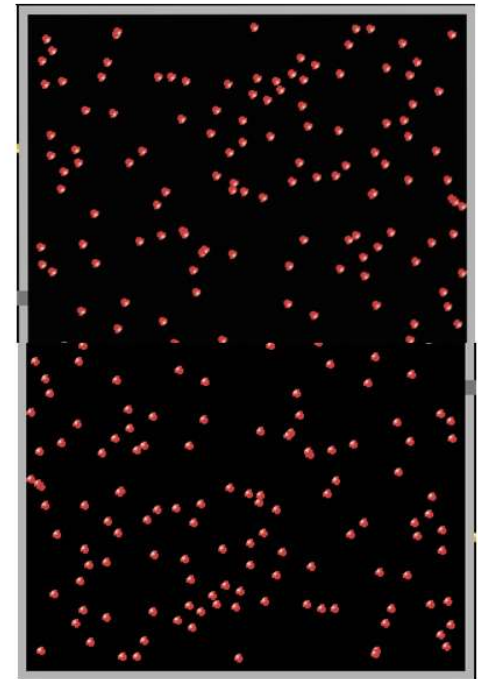
D) None of the above.

Force is double, but
area is also double,
so pressure is the same

1



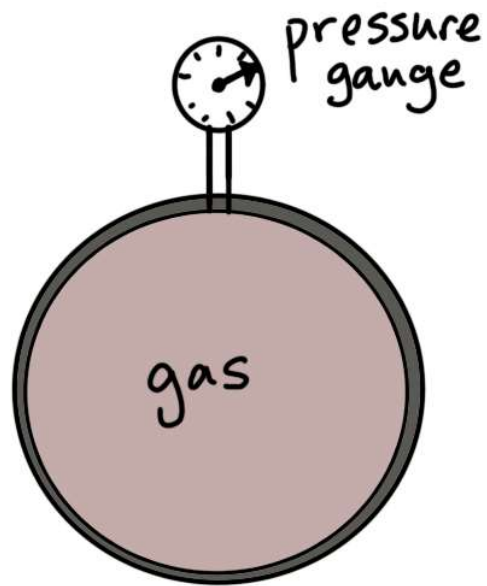
2



EXTRA: faster molecules
more frequent collisions
more impact per collision

Last time in Physics 157...

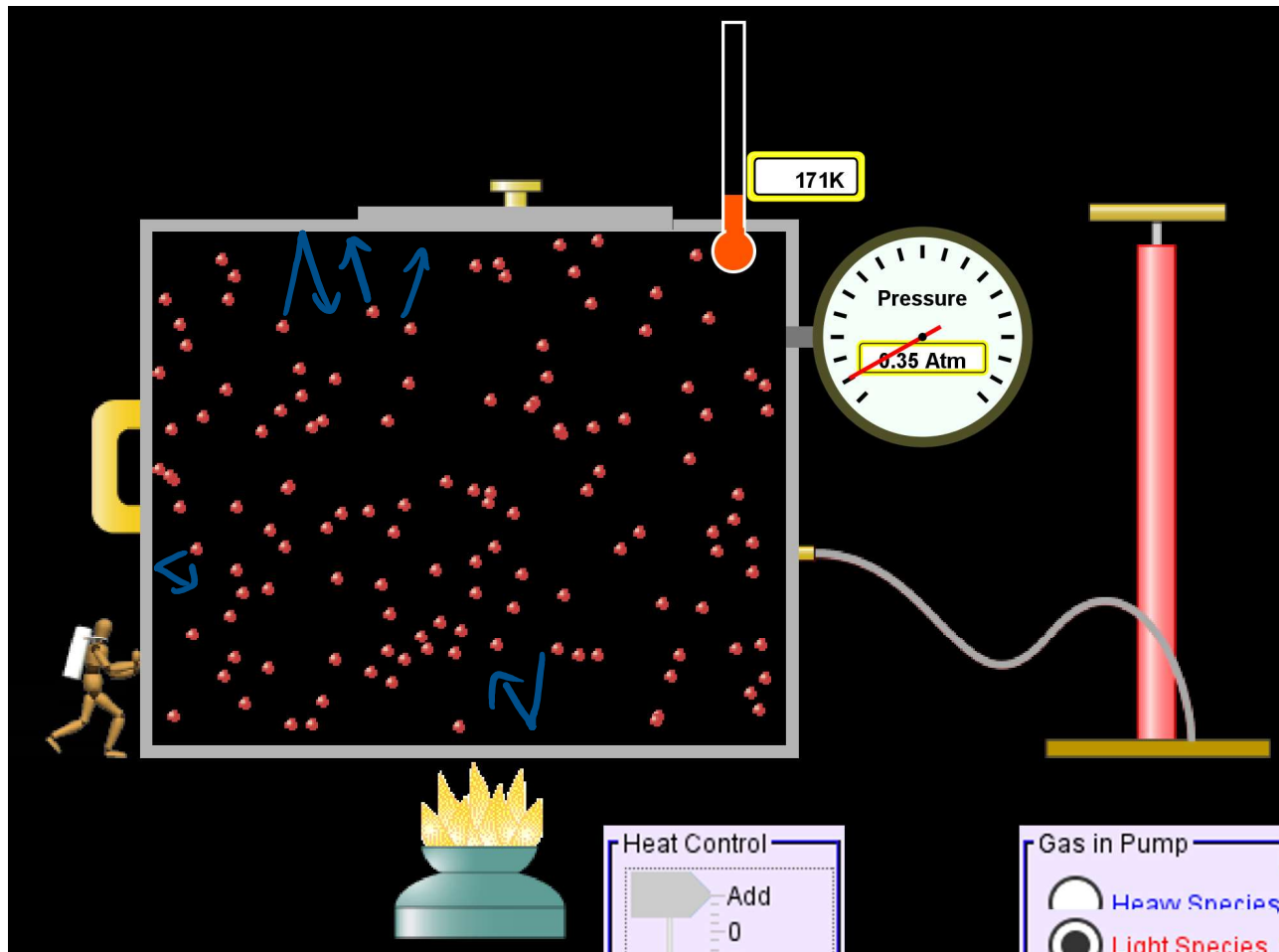
Defining temperature using constant volume gas thermometer



$$P = \text{Force on walls} \\ \text{per unit area}$$

constant
volume
gas thermometer:

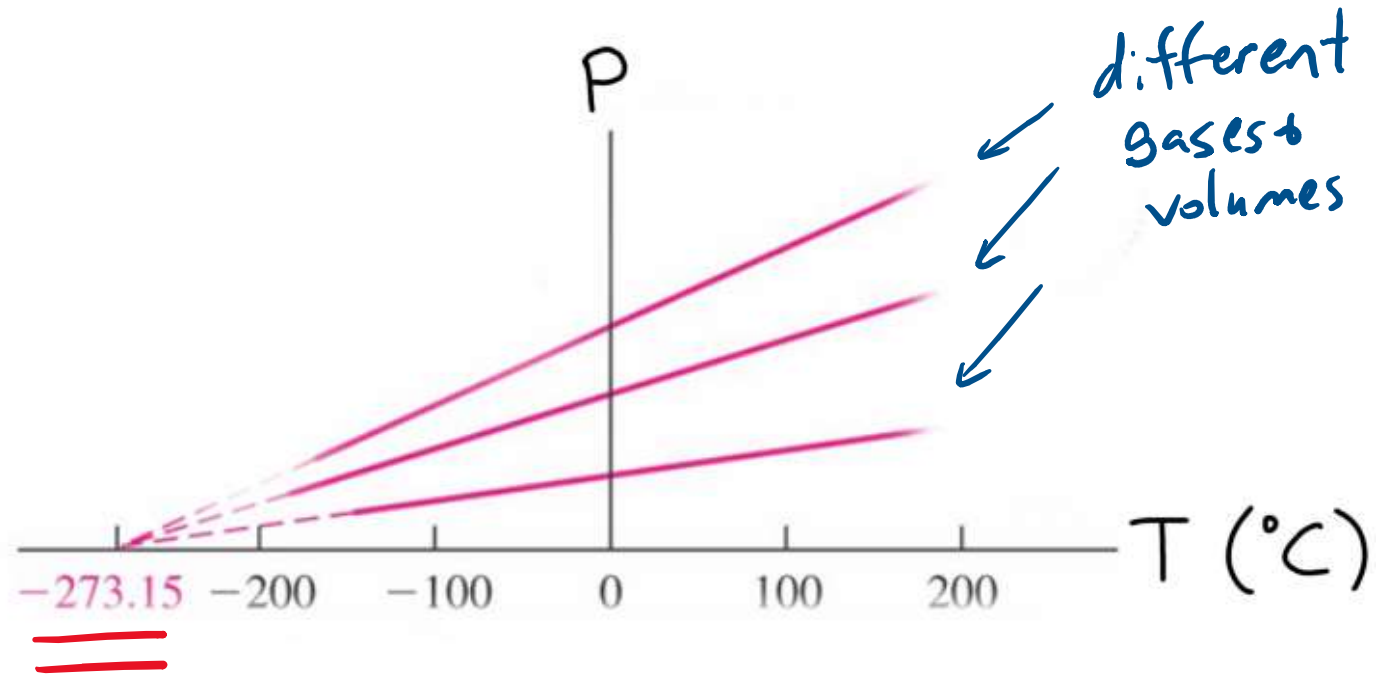
Simulation of an ideal gas : pressure is from the molecules hitting the wall!



As we heat the gas, the molecules move faster so pressure increases.

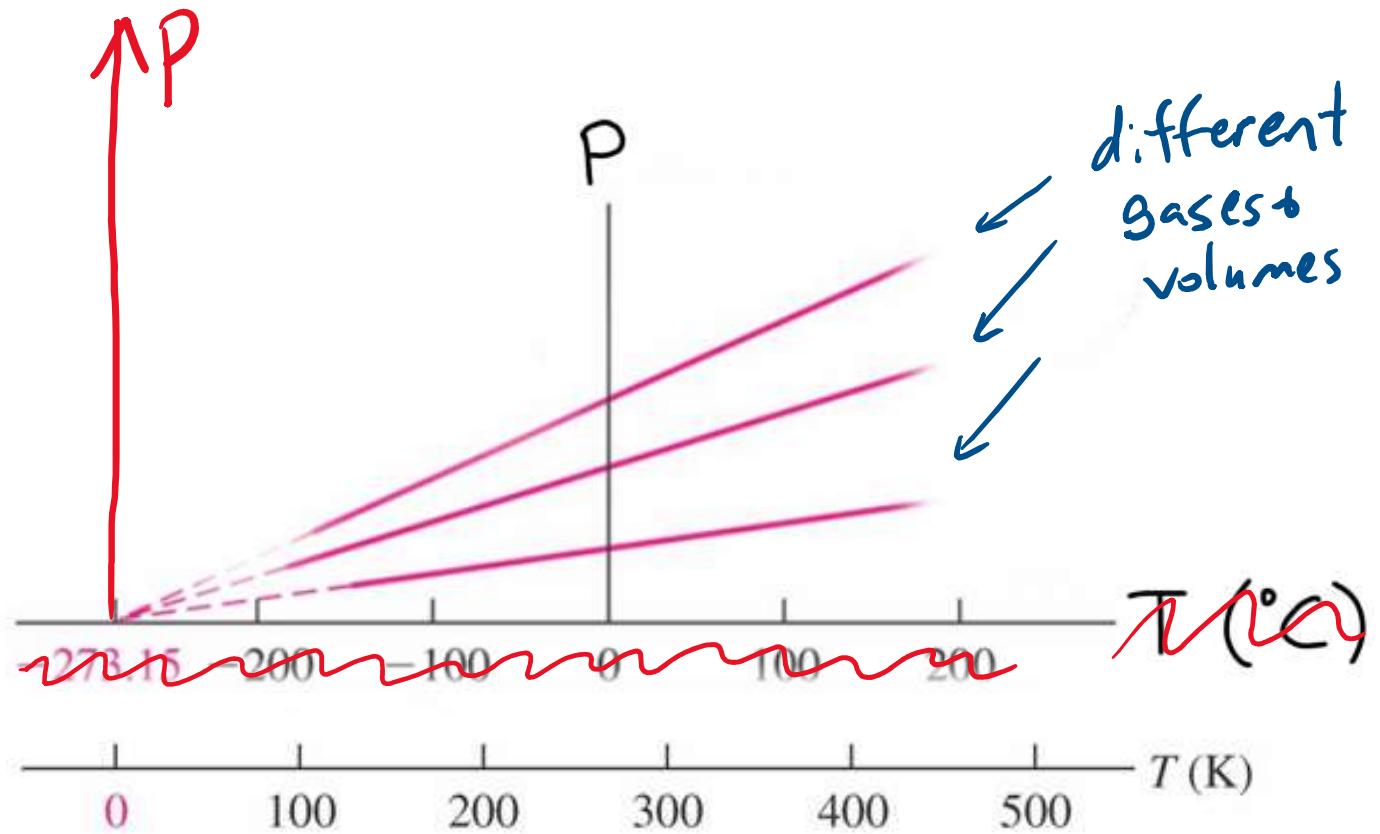
Gas properties PHET from U. Colorado

Pressure vs Celcius temperature for constant volume gas thermometers



Celcius scale: p is LINEAR in T_c $P = mT_c + b$
always extrapolates to $P=0$ at same T

Pressure vs Celcius temperature for constant volume gas thermometers



Kelvin scale: P is proportional to T $P = m \cdot T$

Define Kelvin scale by:

$$T = \text{const.} \times P$$

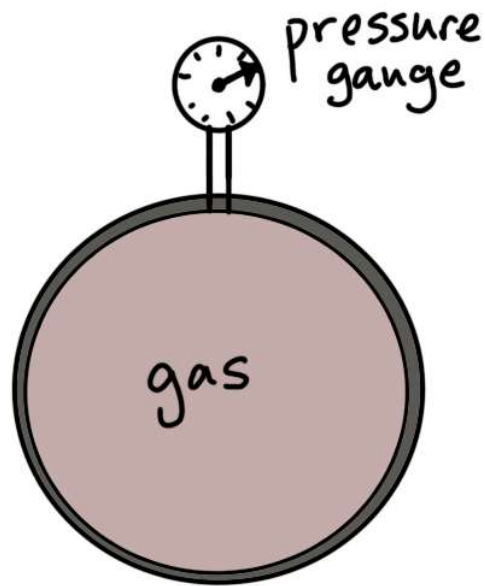
and

↑
depends on
particular thermometer

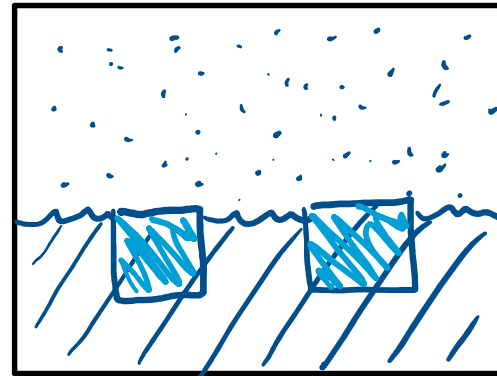
↑
pressure

$$T = 273.16 \text{ K}$$

at triple point of water

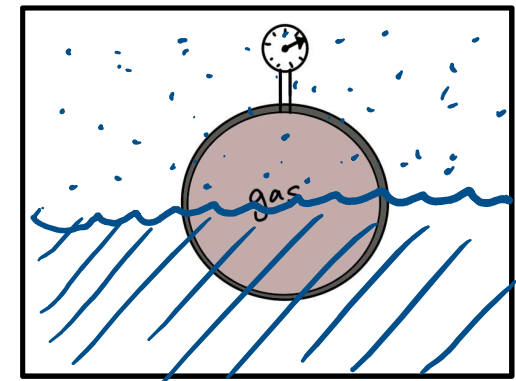
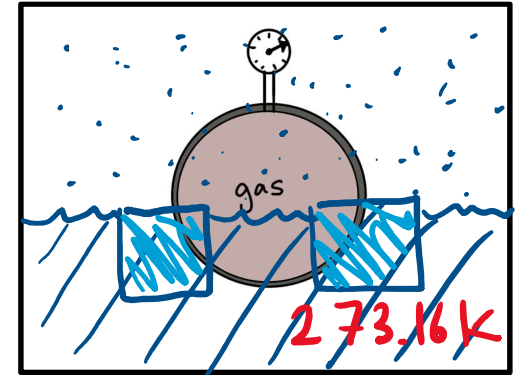


constant
volume
gas thermometer:

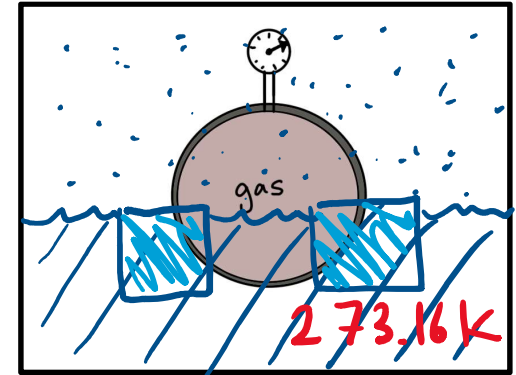


Clicker question: An ideal gas thermometer is calibrated by placing it in equilibrium with water at its triple point. The pressure reads 50kPa. The same thermometer is placed in equilibrium with another container of water. If the pressure reads 100kPa, we can say that the temperature of the water is

- A) 136.58K
- B) 273.16K
- C) 546.32K
- D) 373.00K
- E) We need to know the constant of proportionality between T and P to answer this.



Clicker question: An ideal gas thermometer is calibrated by placing it in equilibrium with water at its triple point. The pressure reads 50kPa. The same thermometer is placed in equilibrium with another container of water. If the pressure reads 100kPa, we can say that the temperature of the water is



A) 136.58K

B) 273.16K

C) 546.32K

D) 373.00K

E) We need to know the constant of proportionality between T and P to answer this.

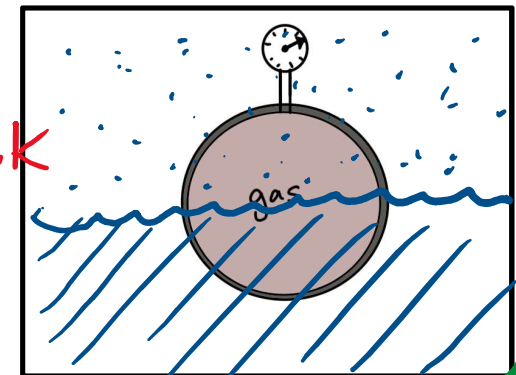
$$T = \text{const} \times P$$

means $\frac{T_2}{T_1} = \frac{P_2}{P_1} = 2$

$$\text{so } T_2 = 2 \cdot 273.16\text{K} = 546.32\text{K}$$

can st

these are equivalent ways to state that T is proportional to P



if $T = c \cdot P$ then :

$$T_1 = c P_1, T_2 = c P_2 \text{ so } \frac{T_1}{T_2} = \frac{P_1}{P_2}$$

Clicker: A 0.010m^3 rigid container of gas has a pressure of 1.0kPa at 20.0°C . The pressure at 120.0°C is closest to:

A. 0.2 kPa

B. 1.3 kPa

C. 3.0 kPa

D. 6.0 kPa

E. There is not enough information to answer.

T_{Celcius} defined as $T_{\text{Kelvin}} + 273.15$

$T_{\text{Fahrenheit}}$ defined as $\frac{9}{5} T_{\text{Celcius}} + 32$

Clicker: A 0.010m^3 rigid container of gas has a pressure of 1.0kPa at 20.0°C . The pressure at 120.0°C is closest to:

A. 0.2 kPa

B. 1.3 kPa

C. 3.0 kPa

D. 6.0 kPa

E. There is not enough information to answer.

$$\frac{P_2}{P_1} = \frac{(T_{\text{kelvin}})_2}{(T_{\text{kelvin}})_1} \approx \frac{4}{3}$$

$// T_c + 273.15$

$$\text{so } P_2 \approx \frac{4}{3} P_1$$

T is not proportional to P
if we use the Celsius scale!

**I DON'T ALWAYS
DO THERMODYNAMICS**

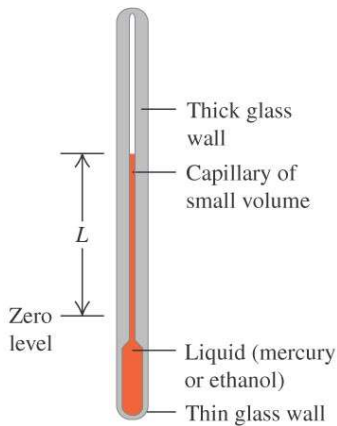


**BUT WHEN I DO,
I USE THE KELVIN SCALE**

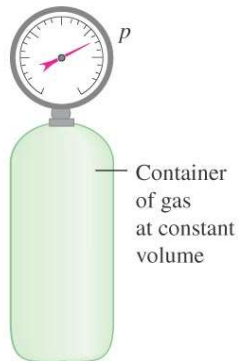
Thermometers

Liquid or gas thermometers

(a) Changes in temperature cause the liquid's volume to change.



(b) Changes in temperature cause the pressure of the gas to change.



Digital



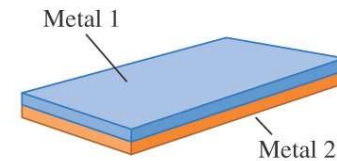
IR (infrared)



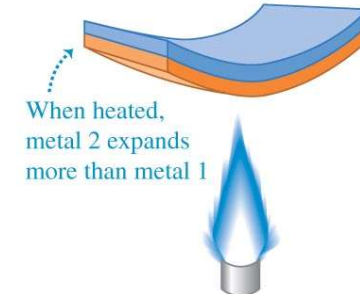
this one doesn't need to be in equilibrium with the sample

Bimetal

(a) A bimetallic strip



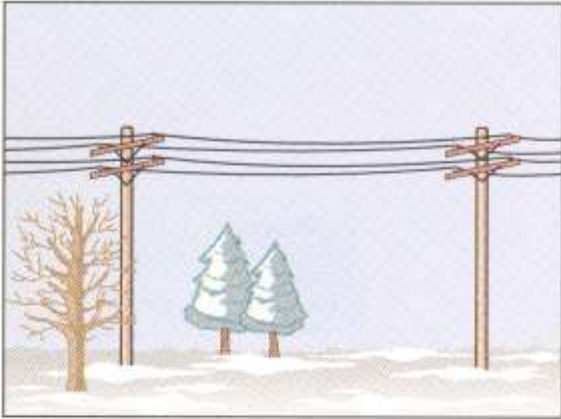
(b) The strip bends when its temperature is raised.



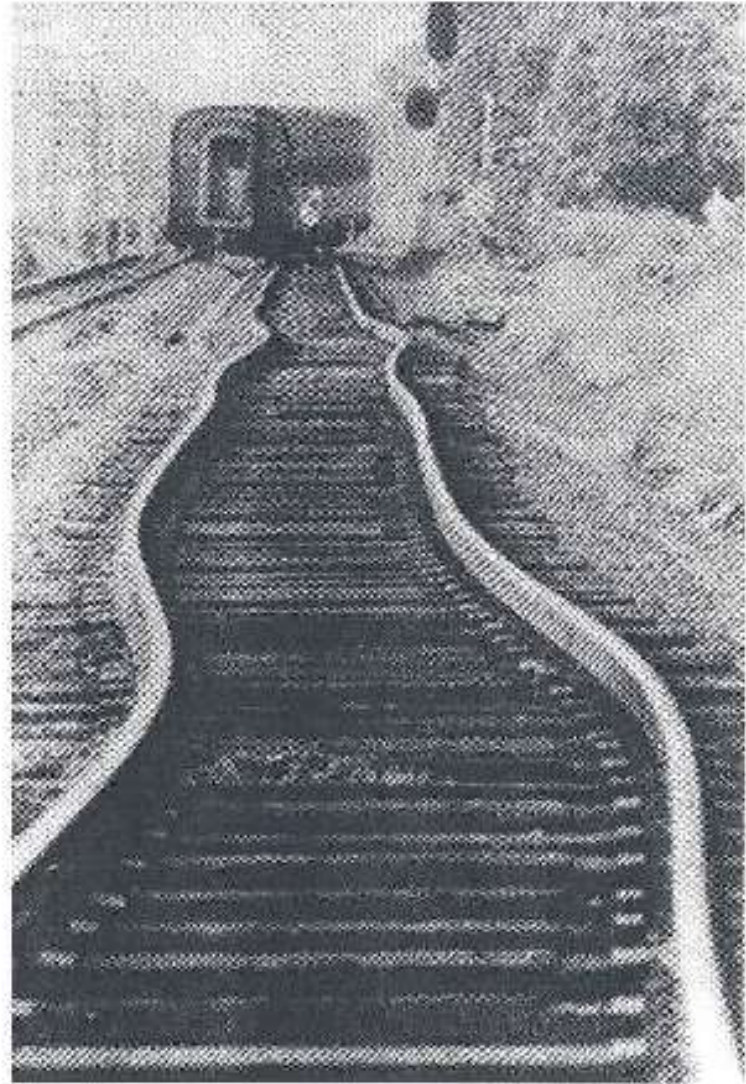
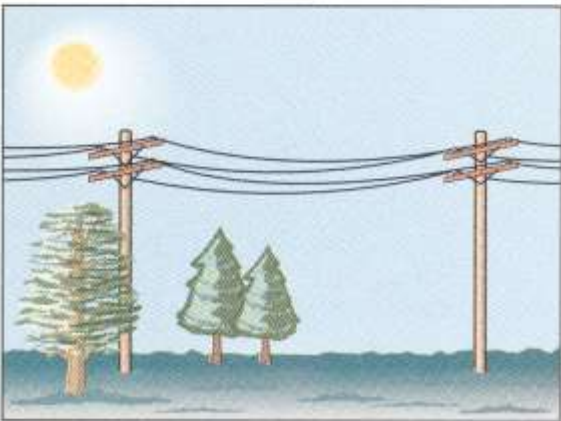
(c) A bimetallic strip used in a thermometer



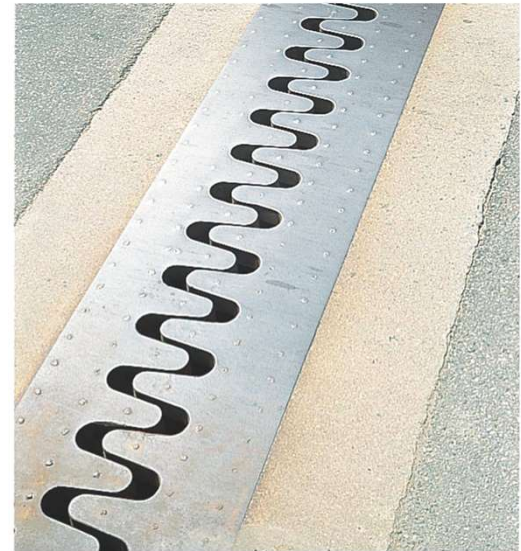
Thermal expansion



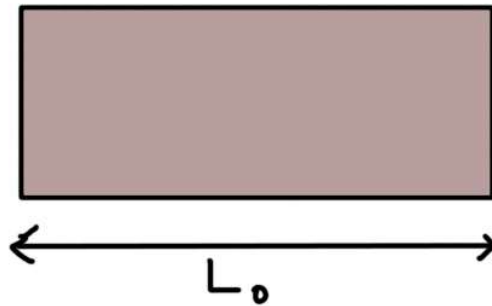
(a)



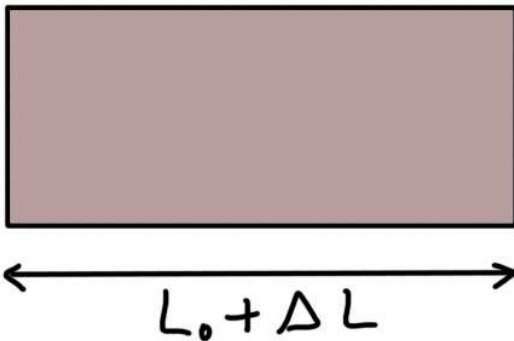
Thermal expansion



Thermal expansion:



temp T



temp $T + \Delta T$

$$\Delta L = \alpha L_0 \Delta T$$

coefficient of linear expansion

- assumes $\frac{\Delta L}{L}$ is small
- α can depend on T

Thermal expansion: Verrazano Narrows Bridge

How much longer will the bridge deck be during the summer compared to the winter?

(center span ~1300m, think order of magnitude)

- A. 5mm
- B. 5cm
- C. 50cm
- D. 5m
- E. 50m

$$\alpha \sim 1 \cdot 10^{-5} \text{ K}^{-1}$$



Photo credit: Tom Giebel, cc licence

$$\Delta L = \alpha L_0 \Delta T$$

Thermal expansion: Verrazano Narrows Bridge

changes in K
are same as
changes in
°C

How much longer will the bridge deck be during the summer compared to the winter?

(center span ~1300m, think order of magnitude)

A. 5mm

B. 5cm

C. 50cm

D. 5m

E. 50m

we only need to be accurate within a factor of 10

$$\Delta T = 50^\circ\text{C} = 50\text{K}$$

(-15°C winter
35°C summer)

$$L_0 = 1300\text{m} \approx 10^3\text{m}$$

$$\alpha = 10^{-5}\text{K}^{-1}$$

$$\alpha \sim 1 \cdot 10^{-5}\text{K}^{-1}$$

$$\Delta L \approx 10^{-5} \times 10^3\text{m} \times 50 = 0.5\text{m}$$

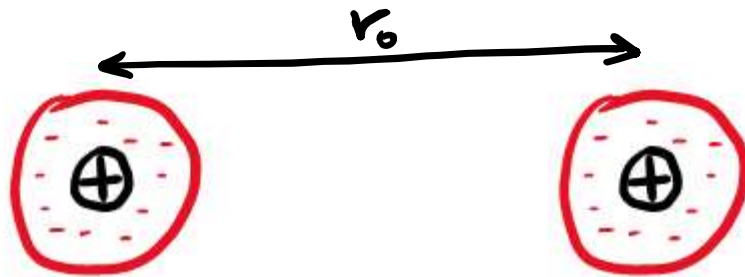
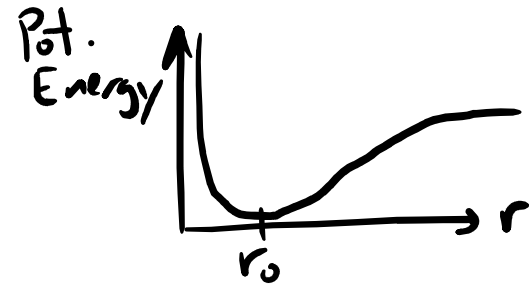


Photo credit: Tom Giebel, cc licence

$$\Delta L = \alpha L_0 \Delta T$$

Why do materials usually expand when heated?

Nearby atoms in solid:



Lowest energy



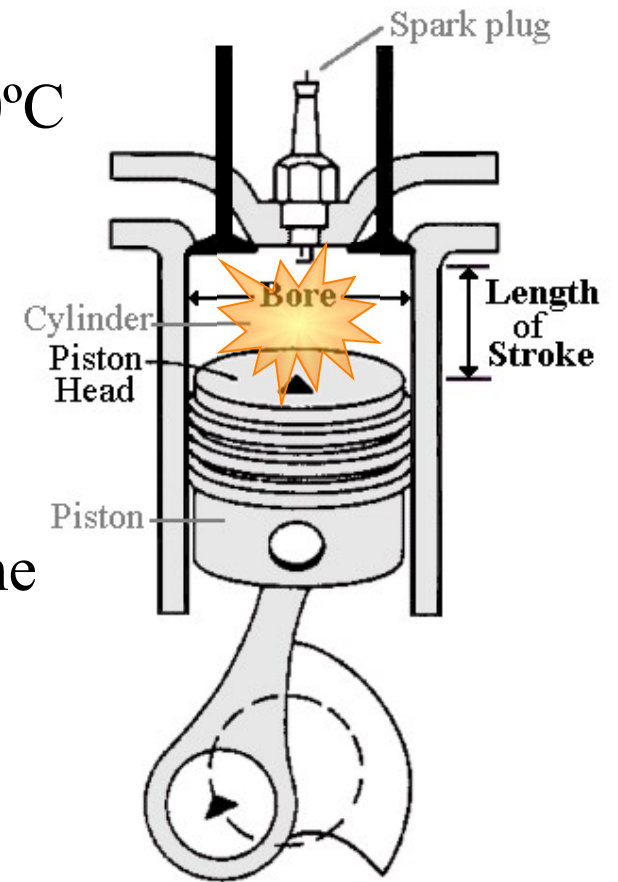
Add energy

More higher energy configurations with $r > r_0$ than $r < r_0$.

Next time: In some car engines, the piston is aluminum ($\alpha = 2.4 \times 10^{-5}$), while the cylinder is cast iron ($\alpha = 1.2 \times 10^{-5}$). If the engine needs to operate between 0°C and 120°C , which of these is a better design:

- A) The piston barely fits in the cylinder at 120°C
- B) The piston barely fits in the cylinder at 0°C

EXTRA: what do we need to worry about if the engine gets too hot? Too cold?



$$\Delta L = \alpha L_0 \Delta T$$

Extra clicker question: At 200K, the pressure of a (nearly) ideal gas in a sealed fixed volume container is 50kPa. The container is now placed in an oven and the pressure is observed to increase to 100kPa. The temperature of the oven is

A) 100K

B) 200K

C) 300K

D) 400K

E) We need to know the constant of proportionality between T and P to answer this.

Clicker question: At 200K, the pressure of a (nearly) ideal gas in a sealed fixed volume container is 50kPa. At 400K, the pressure will be

$$T = \text{const} \cdot P$$

A) 25kPa

B) 50kPa

C) 100kPa

$$\text{means } \frac{P_2}{P_1} = \frac{T_2}{T_1} = 2$$

$$\text{so } P_2 = 2 \cdot 50\text{kPa} = 100\text{kPa}$$

D) we need to know the constant of proportionality between T and P to answer this

We say T is directly proportional to P