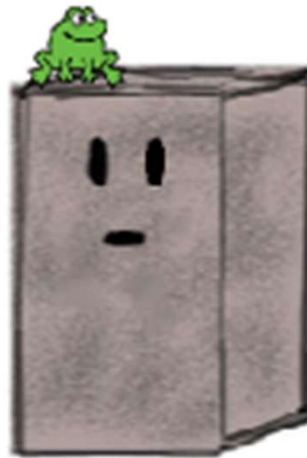
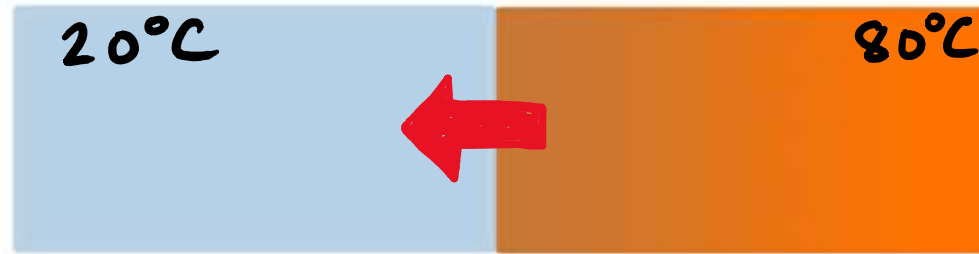




Last time
in Phys 157...



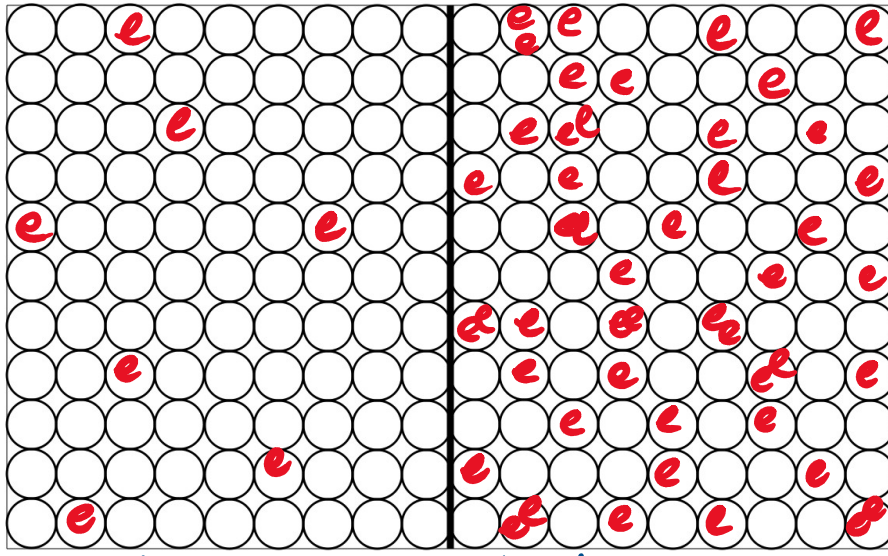
Last time
in Phys 157...



Why does heat always flow from hot objects to colder objects?

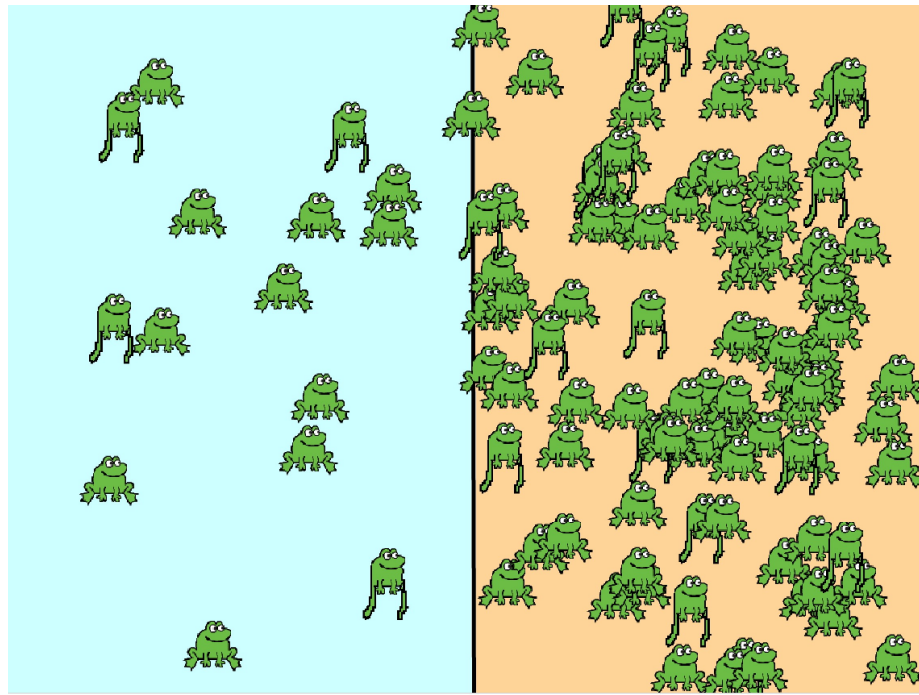
Why can't we make a refrigerator that requires no work done?

Why can't we make an engine that converts heat completely into work?



low T

high T



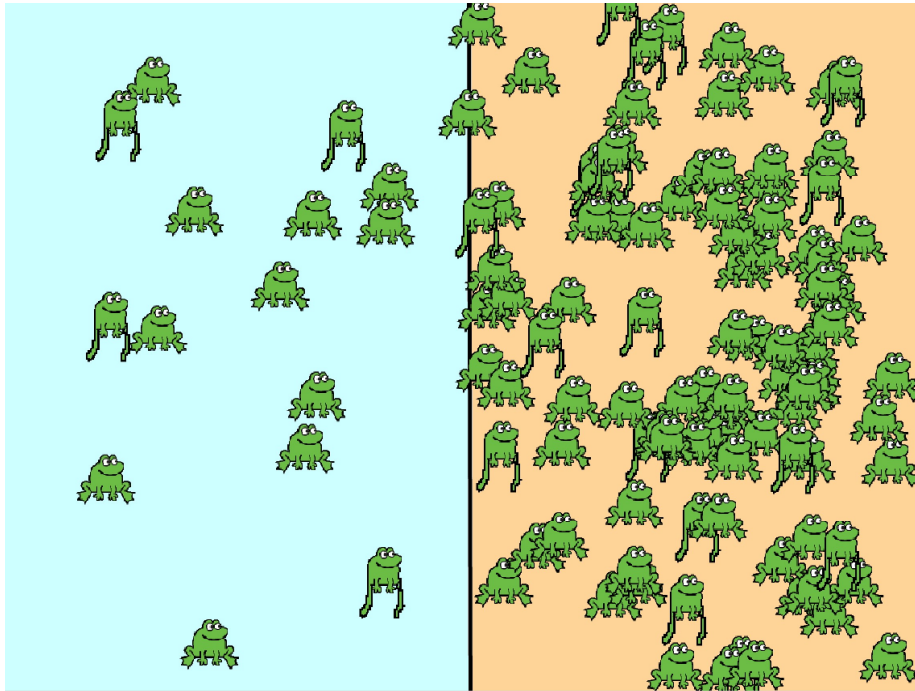
Analogy:

Frogs = energy

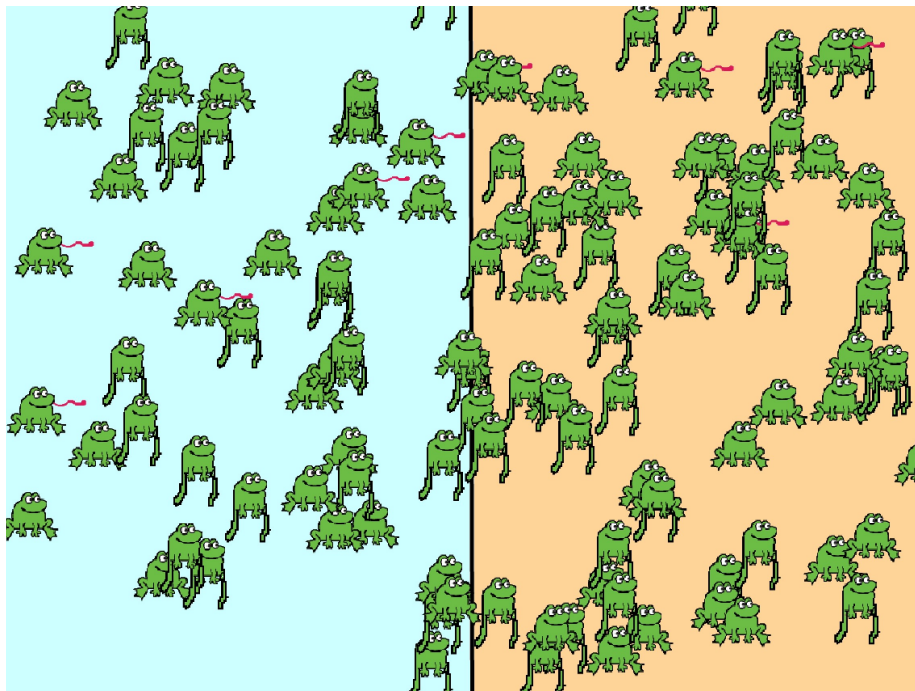
Conserved + move randomly

density of frogs = temperature

↑
proportional to energy per molecule

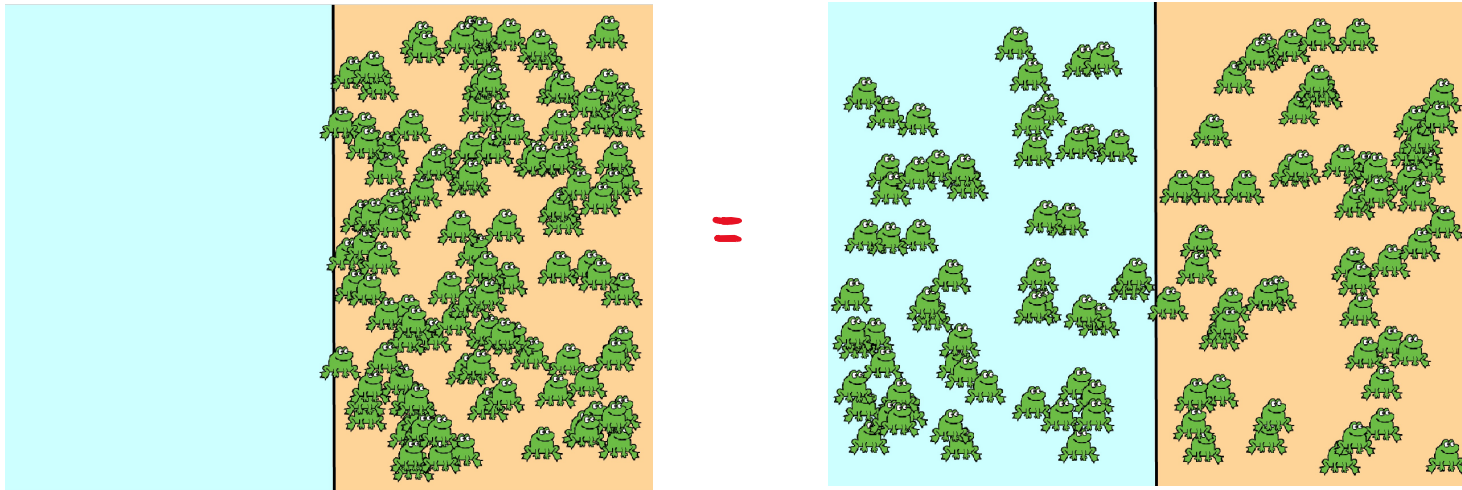


If the frog motion is random, why do we see a net motion of frogs from high density to low density?

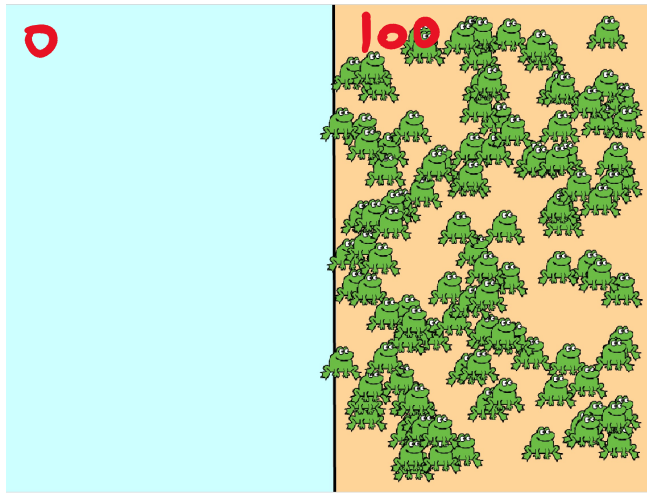


As time passes, we move between possible configurations of frogs.

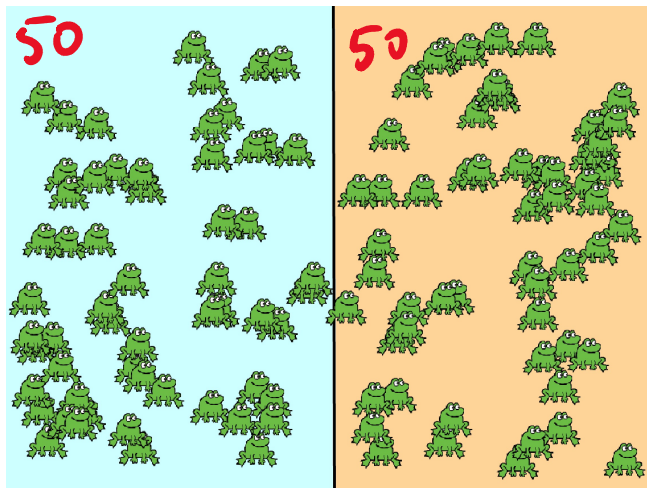
All specific configurations are equally likely



BUT...



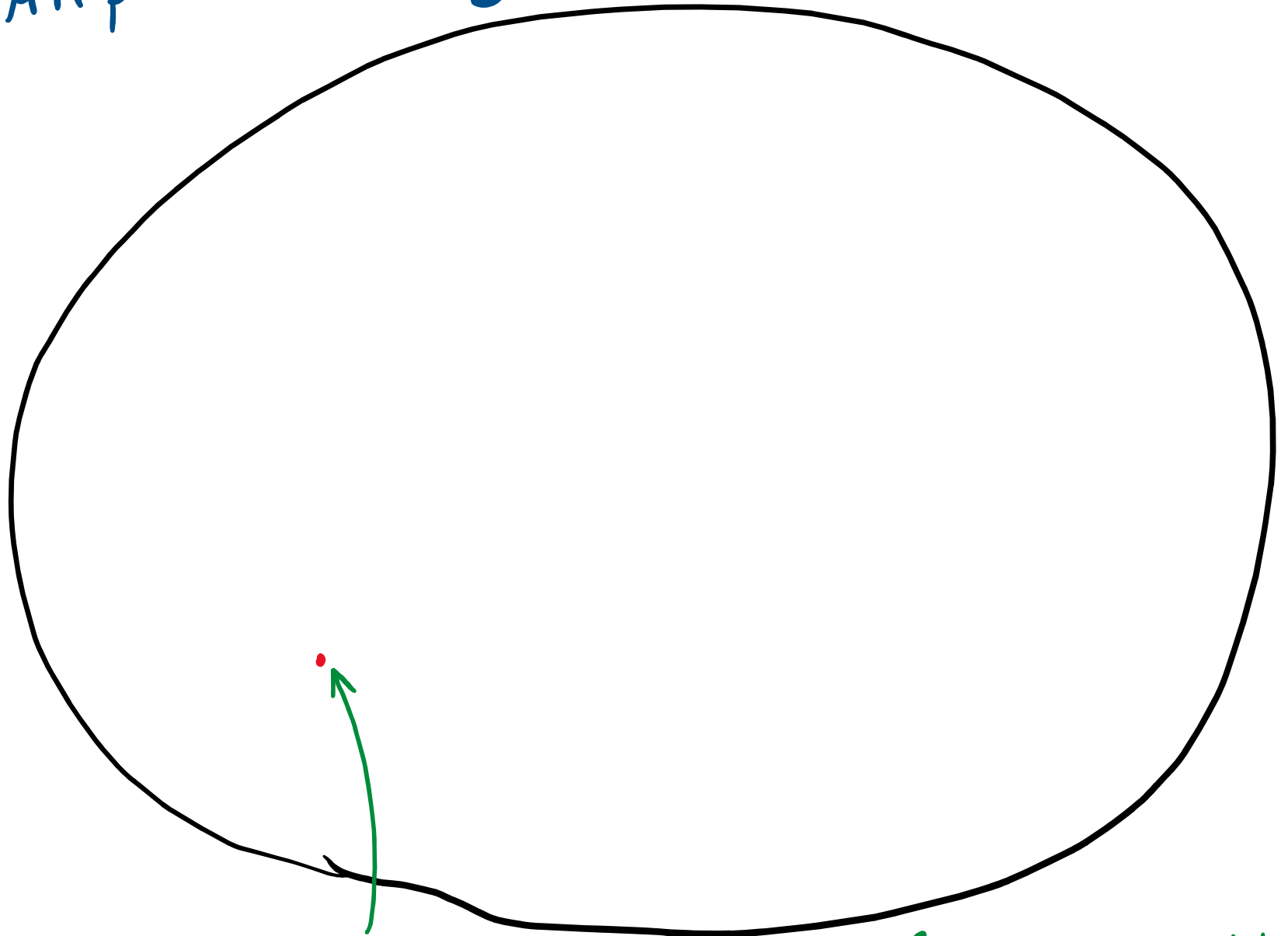
10^{500} configurations
like this



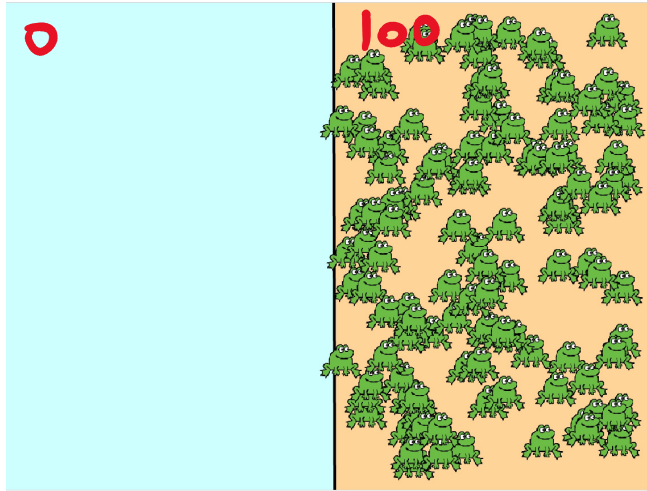
10^{530} configurations
like this

(10^5 possible pixel locations for each frog)

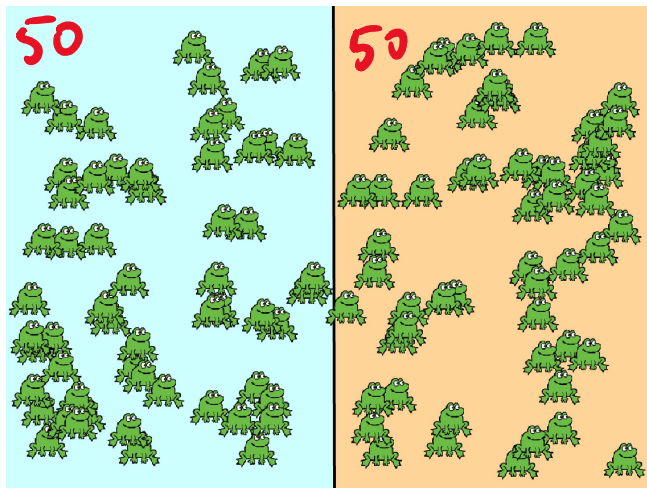
All possible configurations of frogs:



configurations with most of the frogs on the right
 10^{30} times smaller area

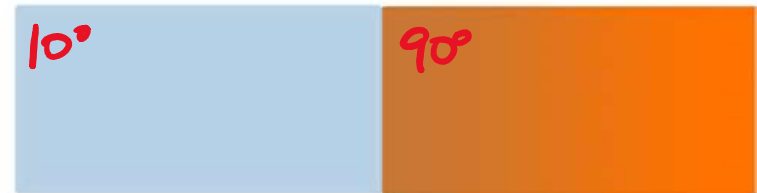
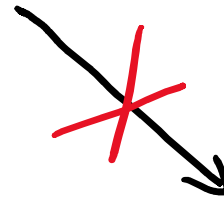
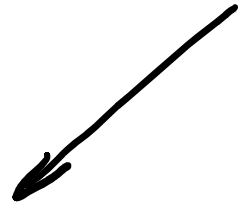


If we start here



After a while, we are 10^{30} times more likely to end up in a (50, 50) configuration than a (0, 100) configuration.

If we start here:



10 | 000 000 000 000 000 000 000 000

times more likely to
end up here.

Define ENTROPY of a macroscopic configuration

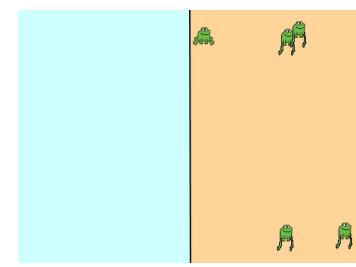
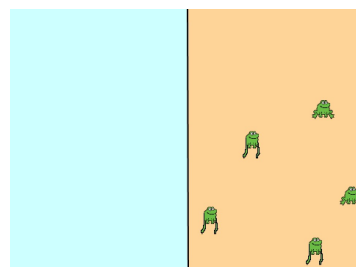
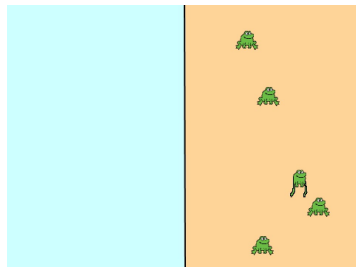
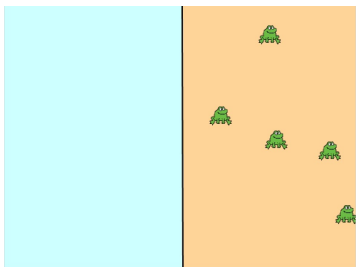
e.g.
(30,70) distribution
of frogs

e.g.2: gas with
pressure P, volume V,
temperature T

$$S = \text{const} \times \ln [N]$$

number of microscopic
configurations of this
type

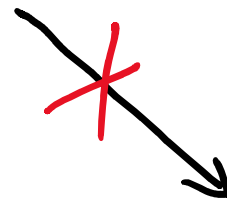
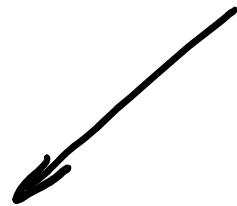
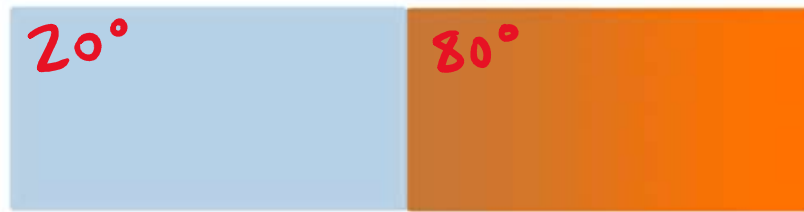
some microscopic configurations of frogs with ^{macroscopic} configuration (0,5)



2ND LAW OF THERMODYNAMICS:

Total entropy never decreases.

↳ probability of decrease
is unimaginably small

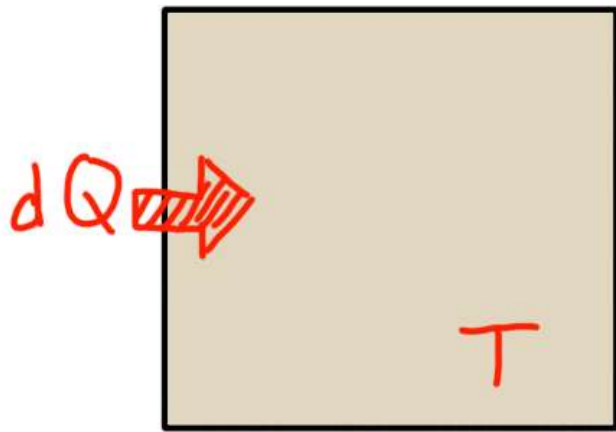


higher entropy
= far more states with these T_s



lower entropy
= far less states w. these T_s .

ENTROPY: macroscopic definition



$$dS = \frac{dQ}{T}$$

change in entropy

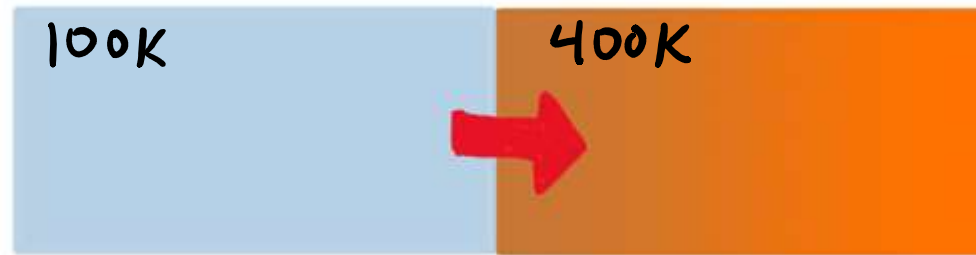
heat added

Amazing result:

we can prove this from the microscopic definition of S .

★ see bonus video ★

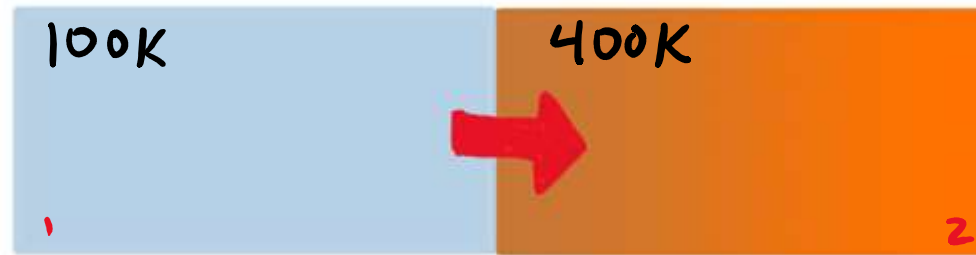
<https://www.youtube.com/watch?v=t7gyi8NhgYg>



Suppose that we had 1J of energy flow from the cold object to the hotter object. What would be the change in entropy of the whole system?

- A) -0.0125 J/K
- B) -0.0075 J/K
- C) 0
- D) 0.0075 J/K
- E) 0.0125 J/K

$$dS = \frac{dQ}{T}$$



Suppose that we had 1J of energy flow from the cold object to the hotter object. What would be the change in entropy of the whole system?

- A) -0.0125 J/K
- B) -0.0075 J/K
- C) 0
- D) 0.0075 J/K
- E) 0.0125 J/K

$$\begin{aligned}
 \text{Have } dS &= dS_1 + dS_2 \\
 &= \frac{dQ_1}{T_1} + \frac{dQ_2}{T_2} \\
 &= \frac{-1\text{J}}{100\text{K}} + \frac{1\text{J}}{400\text{K}}
 \end{aligned}$$

$$= -0.0075 \text{ J/K}$$

BAD

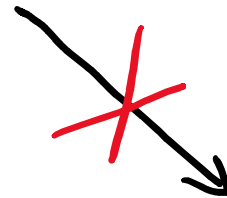
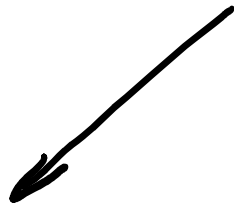
violates 2nd Law so won't happen

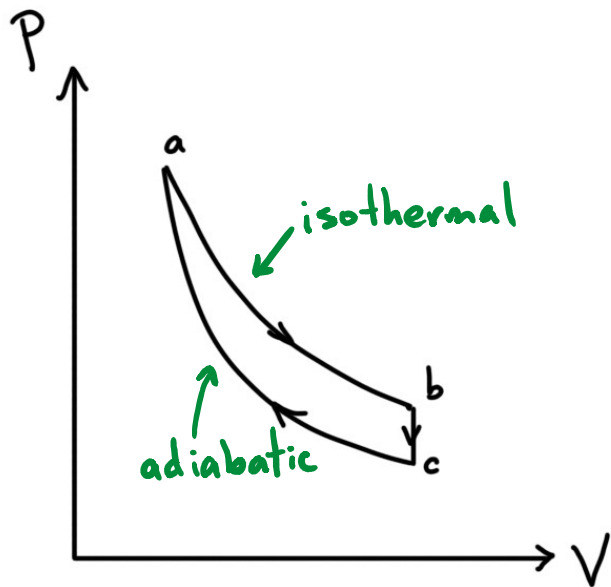
$$dS = \frac{dQ}{T}$$

2ND LAW OF THERMODYNAMICS:

Total entropy never decreases.

→ probability of decrease is too small to comprehend

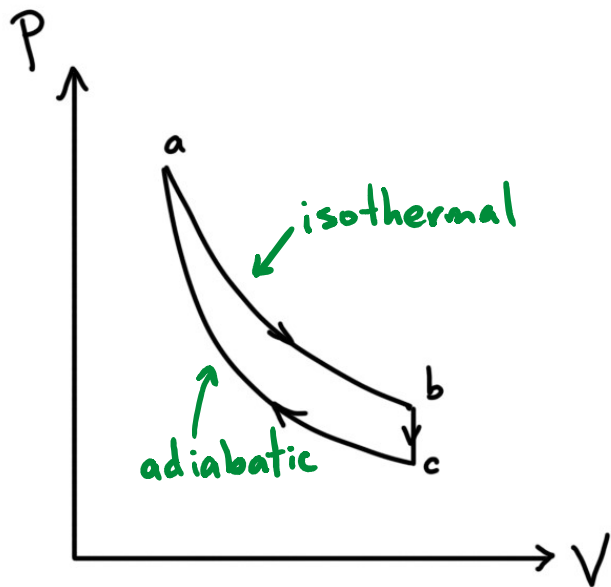




In the cycle shown, we can say that from c \rightarrow a,

- A) The entropy increases
- B) The entropy is constant
- C) The entropy decreases

$$dS = \frac{dQ}{T}$$



In the cycle shown, we can say that from $c \rightarrow a$,

A) The entropy increases

B) The entropy is constant

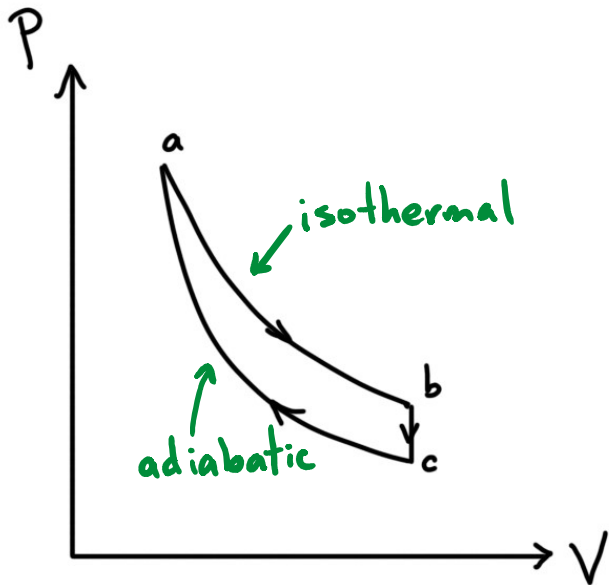
C) The entropy decreases

$c \rightarrow a$ adiabatic so $Q = 0$

$dQ = 0$ for each part so

$dS = 0$

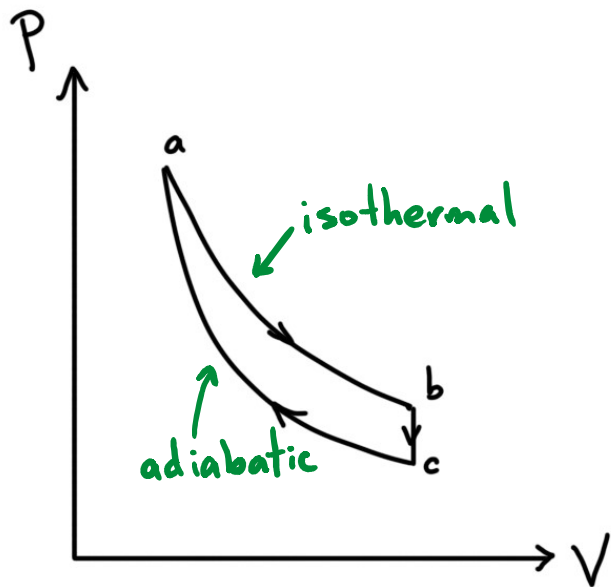
$$dS = \frac{dQ}{T}$$



In the cycle shown, heat Q enters the gas in the isothermal step $a \rightarrow b$ at temperature T . The entropy change during this step

- A) is equal to Q/T .
- B) Is equal to 0.
- C) is equal to $-Q/T$.
- D) cannot be determined from the information provided.

$$dS = \frac{dQ}{T}$$



In the cycle shown, heat Q enters the gas in the isothermal step $a \rightarrow b$ at temperature T . The entropy change during this step

A) is equal to Q/T .

B) Is equal to 0.

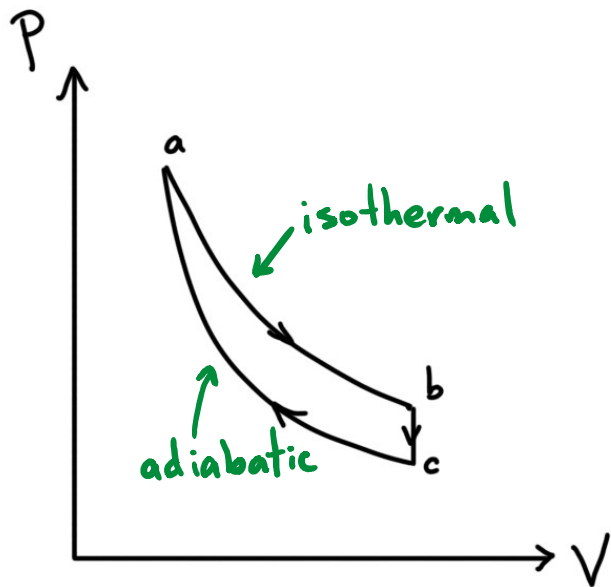
C) is equal to $-Q/T$.

D) cannot be determined from the information provided.

T const. so

$$\Delta S = \frac{Q}{T}$$

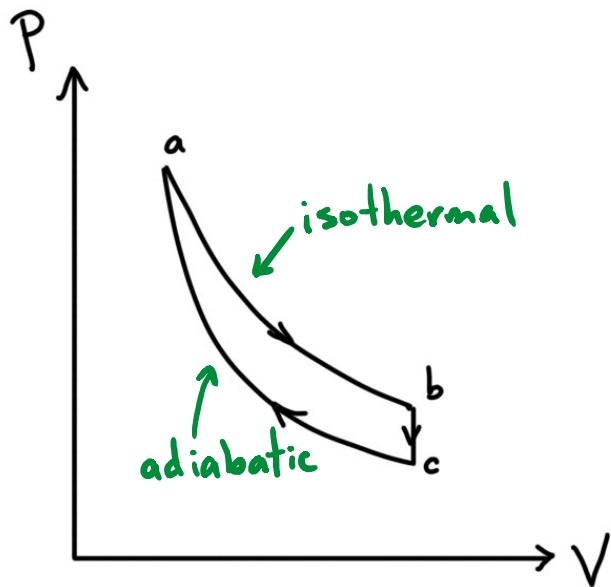
$$dS = \frac{dQ}{T}$$



In the cycle shown, heat Q enters the gas in the isothermal step $a \rightarrow b$ at temperature T . The entropy change from $b \rightarrow c$ is

- A) Q/T
- B) Between 0 and Q/T
- C) 0
- D) Between $-Q/T$ and 0
- E) $-Q/T$

$$dS = \frac{dQ}{T}$$



In the cycle shown, heat Q enters the gas in the isothermal step $a \rightarrow b$ at temperature T . The entropy change from $b \rightarrow c$ is

- A) Q/T
- B) Between 0 and Q/T
- C) 0
- D) Between $-Q/T$ and 0

$$S_c = S_a \text{ since } c \rightarrow a \text{ adiabatic}$$

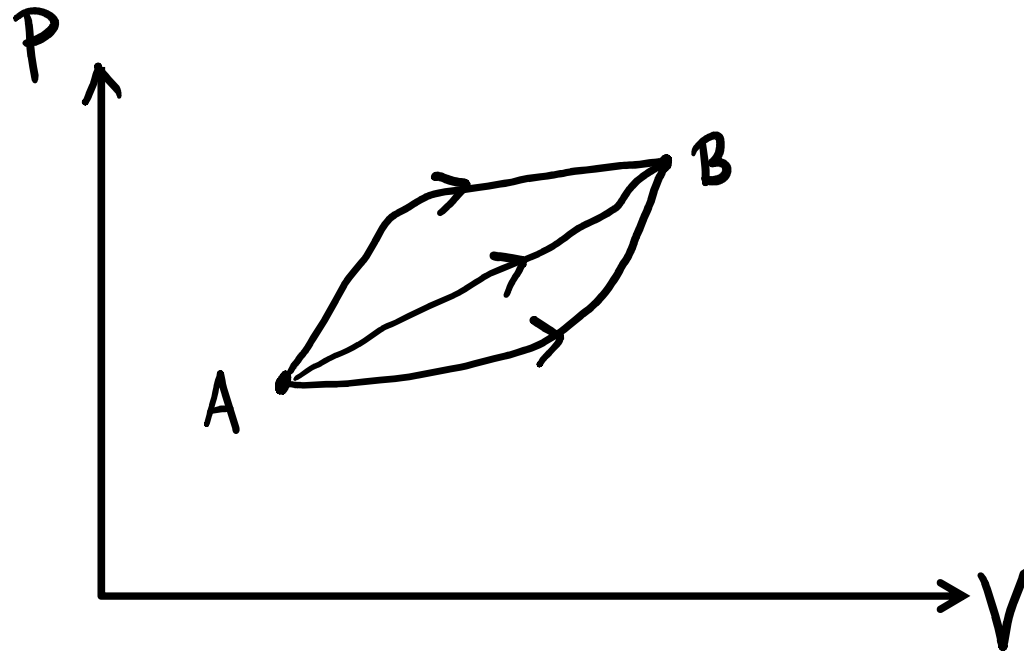
$$\text{so } \Delta S_{a \rightarrow b} + \Delta S_{b \rightarrow c} = 0$$

$$\begin{aligned} \Delta S_{b \rightarrow c} &= -\Delta S_{a \rightarrow b} \\ &= -\frac{Q}{T} \end{aligned}$$

E) $-Q/T$

$$dS = \frac{dQ}{T}$$

Entropy is a state variable - like P, V, T, U



ΔS same for all paths, zero for cycle.

But: S for environment usually increases!