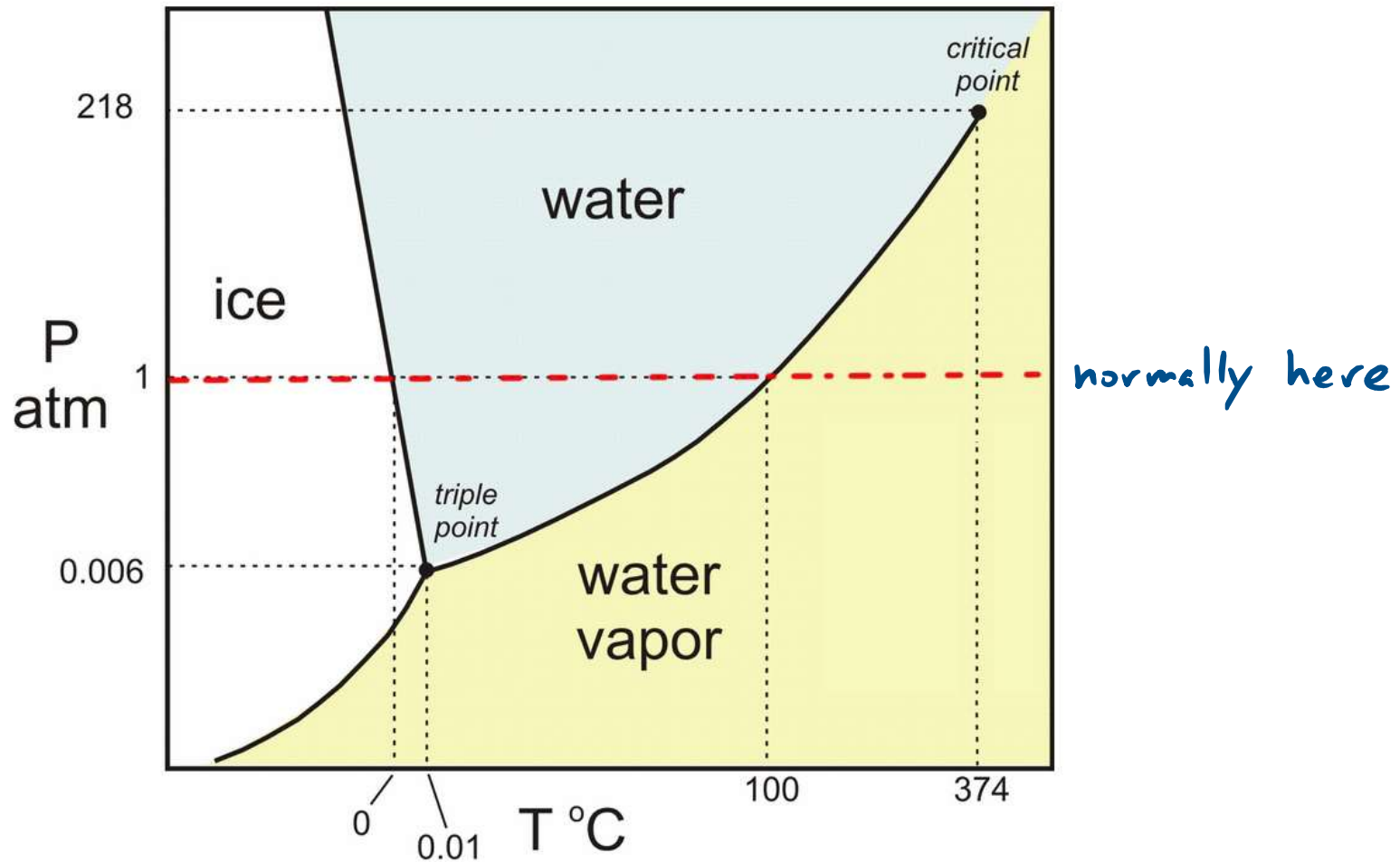


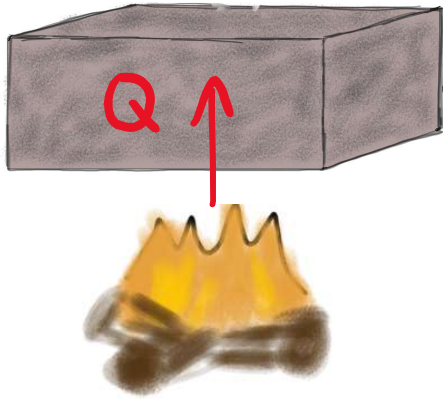
A mass M of ice at temperature $T_1 < 0$ is heated until we have water at temperature $T_2 > 0$. How much heat has been added?

- A) $M c_{\text{ice}} (T_2 - T_1)$
- B) $M c_{\text{water}} (T_2 - T_1)$
- C) $M L_f$
- D) $M c_{\text{ice}} (-T_1) + M c_{\text{water}} (T_2)$
- E) $M c_{\text{ice}} (-T_1) + M L_f + M c_{\text{water}} (T_2)$

PHASE DIAGRAM: displays phases and phase transition curves as a function of T and P



Heat required to raise the temperature of a material determined by its SPECIFIC HEAT c :



heat added \swarrow mass \swarrow

$$Q = m c \Delta T$$

OR:

\swarrow

$$Q = n C \Delta T$$

moles \swarrow

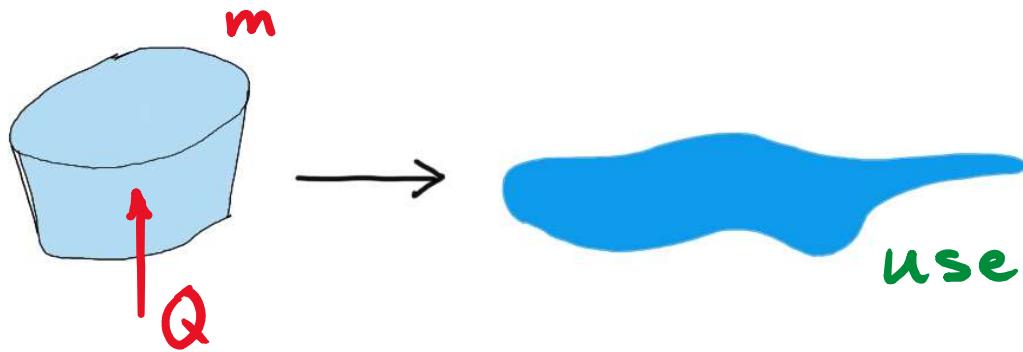
\uparrow
MOLAR SPECIFIC HEAT
= MOLAR HEAT CAPACITY

LATENT HEAT: Heat required to melt / boil a mass m of material (at melting / boiling point) is:

$$Q = mL$$

mass

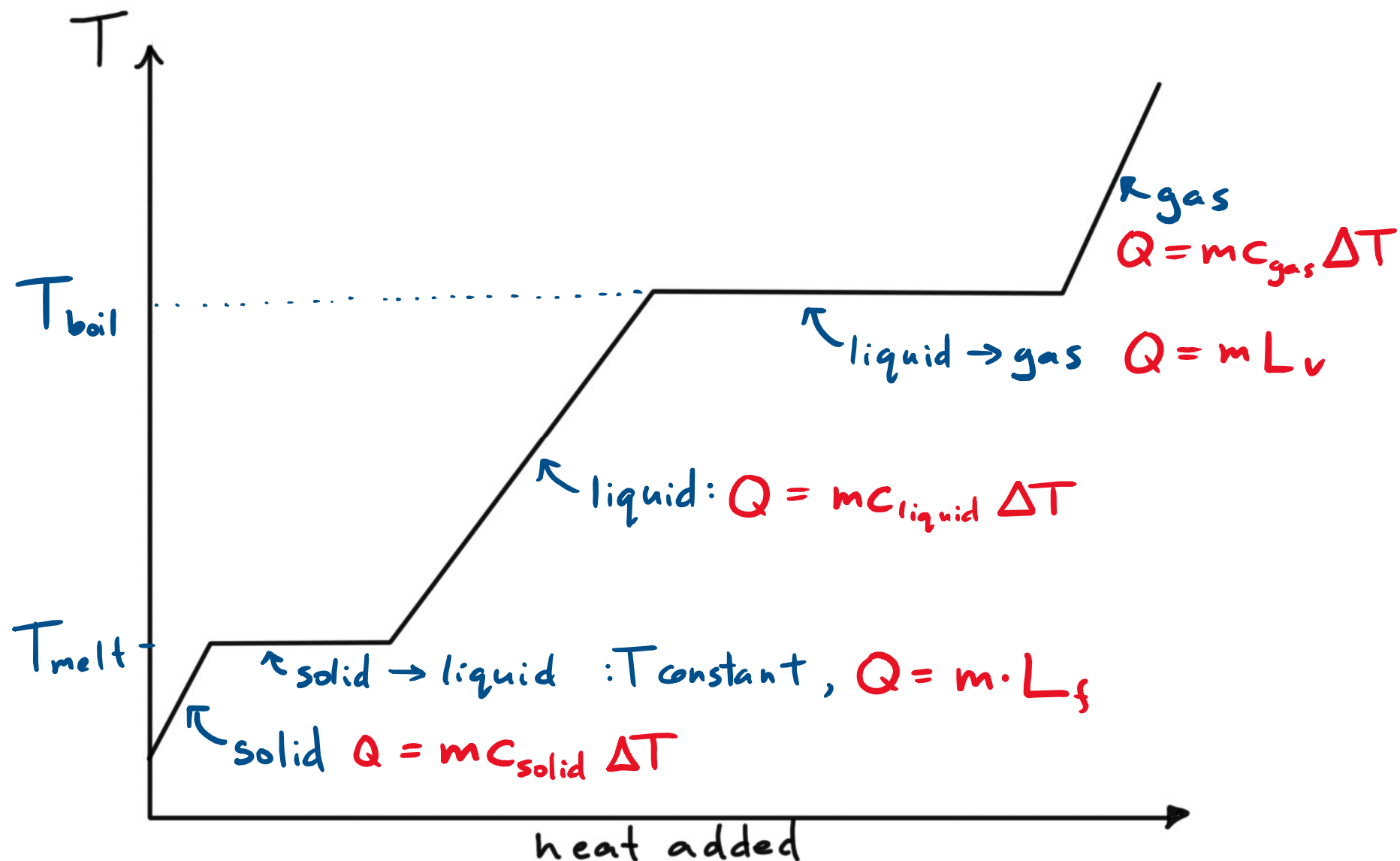
latent
heat

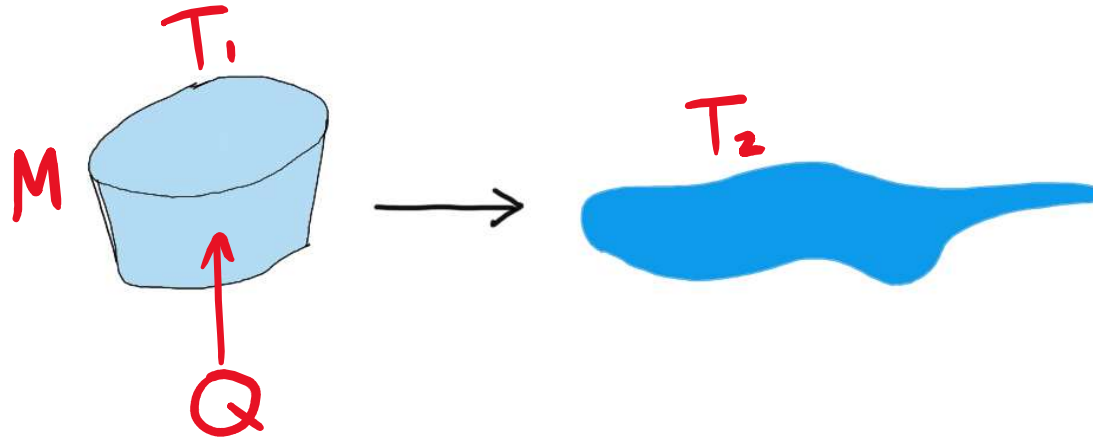


use L_f for melting/freezing

L_v for boiling/condensing

T vs heat added (e.g. water at atmospheric pressure)





A mass M of ice at temperature $T_1 < 0$ is heated until we have water at temperature $T_2 > 0$. How much heat has been added?

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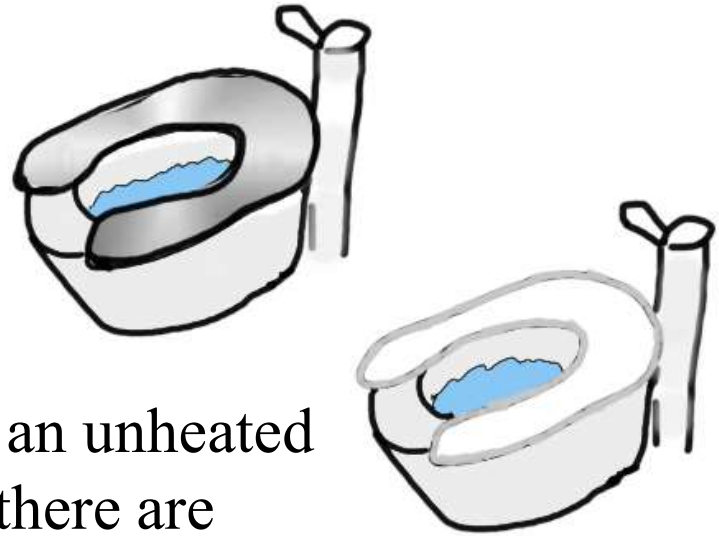
D) $M c_{\text{ice}} (-T_1) + M c_{\text{water}} (T_2)$

E) $M c_{\text{ice}} (-T_1) + M L_f + M c_{\text{water}} (T_2)$

\uparrow
 Q to heat ice
from T_1 to 0°C

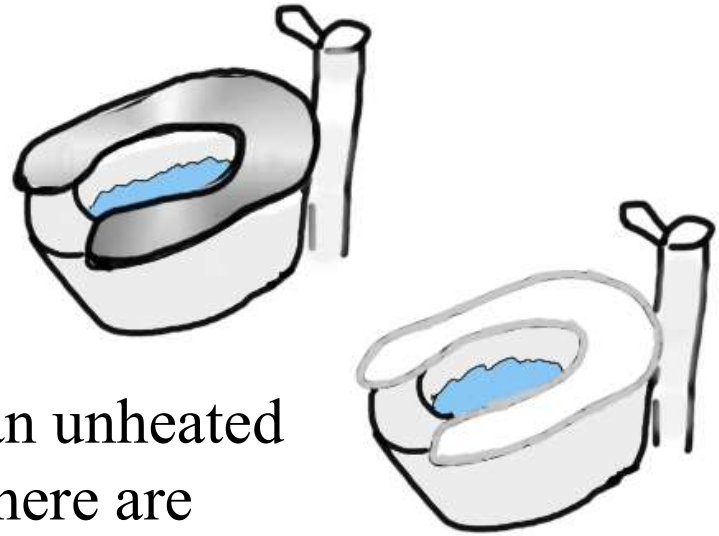
\uparrow
 Q to
melt

\uparrow
 Q to heat from 0°C
water to T_2



During a break from skiing, you enter an unheated washroom building (0°C). You notice there are two toilets, one with a metal seat ($c \sim 200 \text{ J/kg}\cdot\text{K}$) and one with a plastic seat ($c \sim 1600 \text{ J/kg}\cdot\text{K}$). Assuming that you need to sit down, and that both seats are clean, which do you choose?

- A) The metal seat.
- B) The plastic seat.
- C) It doesn't matter: they are the same temperature.
- D) My head says A) but my heart says B).

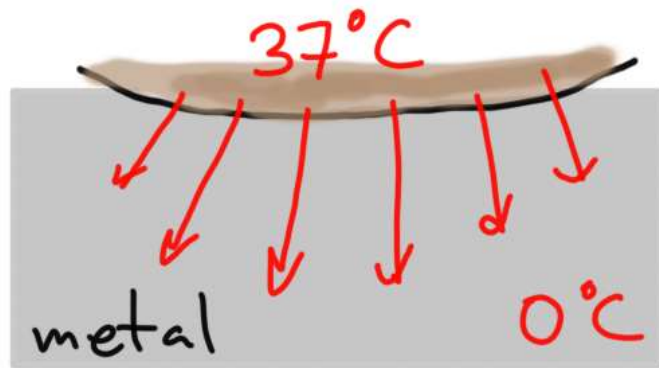


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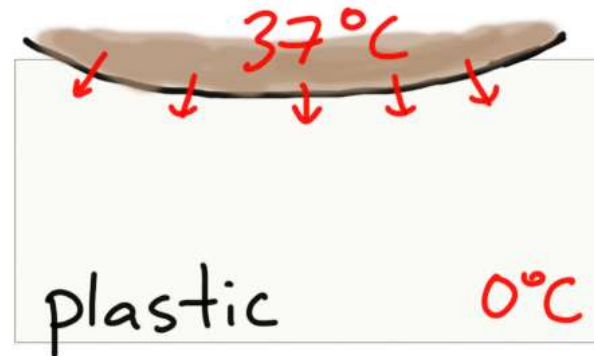
- A) The metal seat.
- B) The plastic seat.
- C) It doesn't matter: they are the same temperature.
- D) My head says A) but my heart says B).

I'm not here to give you advice about using the bathroom, but personally, I would go for the plastic one.

THERMAL CONDUCTIVITY: Heat moves more quickly through some materials than others in response to a temperature gradient.



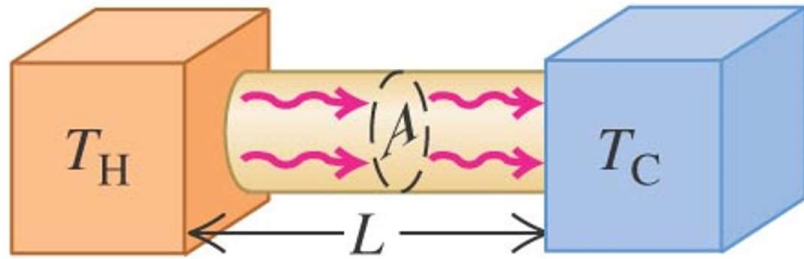
good thermal
conductor



poor thermal
conductor (insulator)

- the metal feels colder since it cools our skin quicker

THERMAL CONDUCTIVITY: Determines heat current from temperature gradient.



cross sectional area

$$H = k A \frac{T_H - T_C}{L}$$

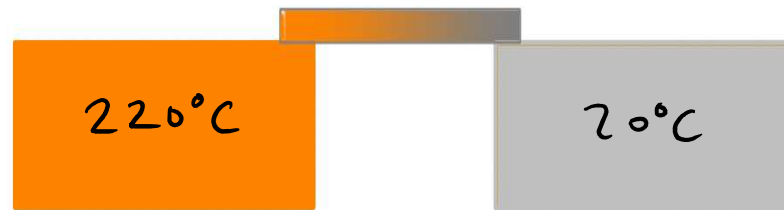
temperature gradient

calculus version: $\frac{dT}{dx}$

Heat current
(Joules/second)

Thermal conductivity = basic property of a material

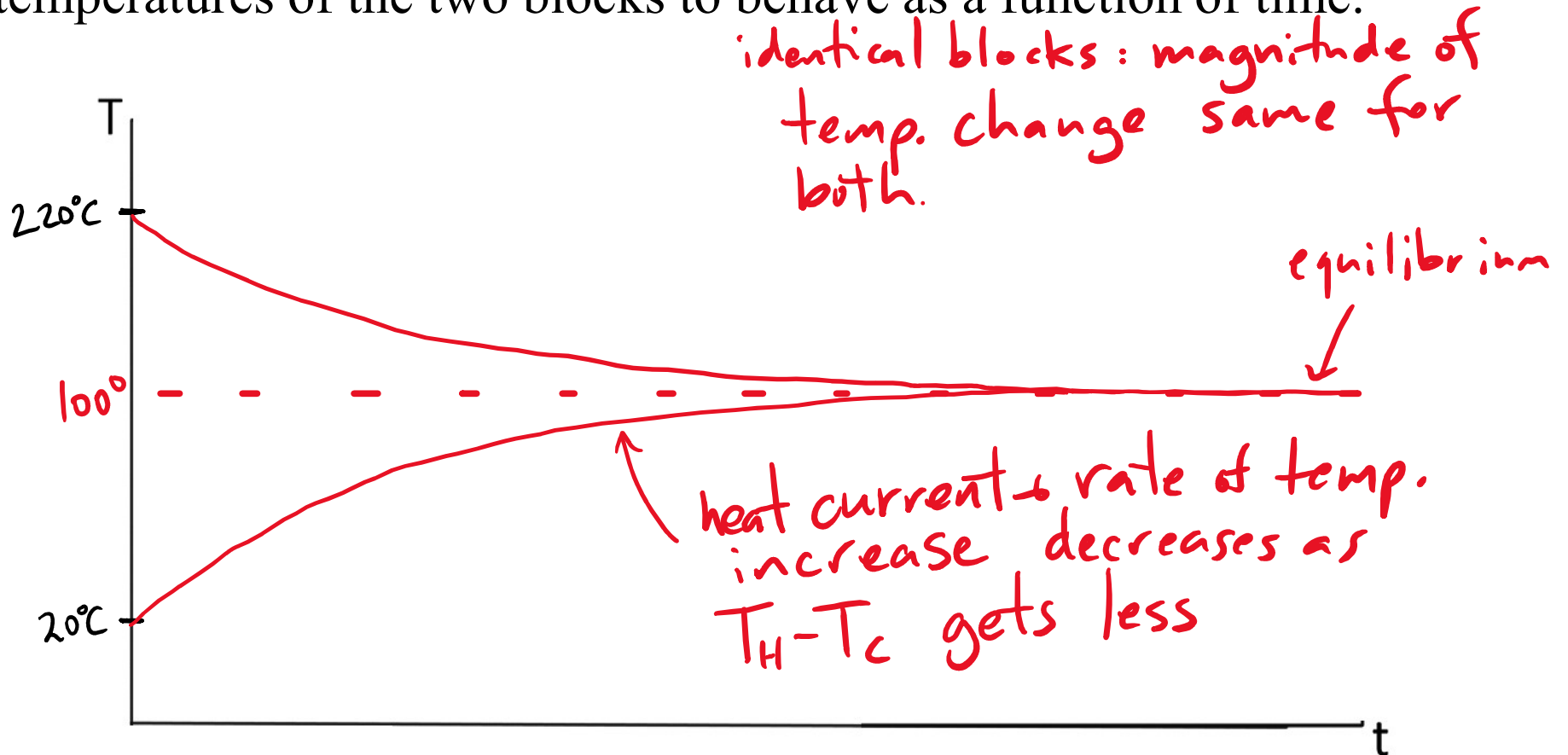
Conductivity worksheet



A block of aluminum at room temperature ($T_1 = 20^{\circ}\text{C}$) is connected to another equivalent block of aluminum at ($T_2 = 220^{\circ}\text{C}$) by another strip of aluminum (that has been in place for a while).

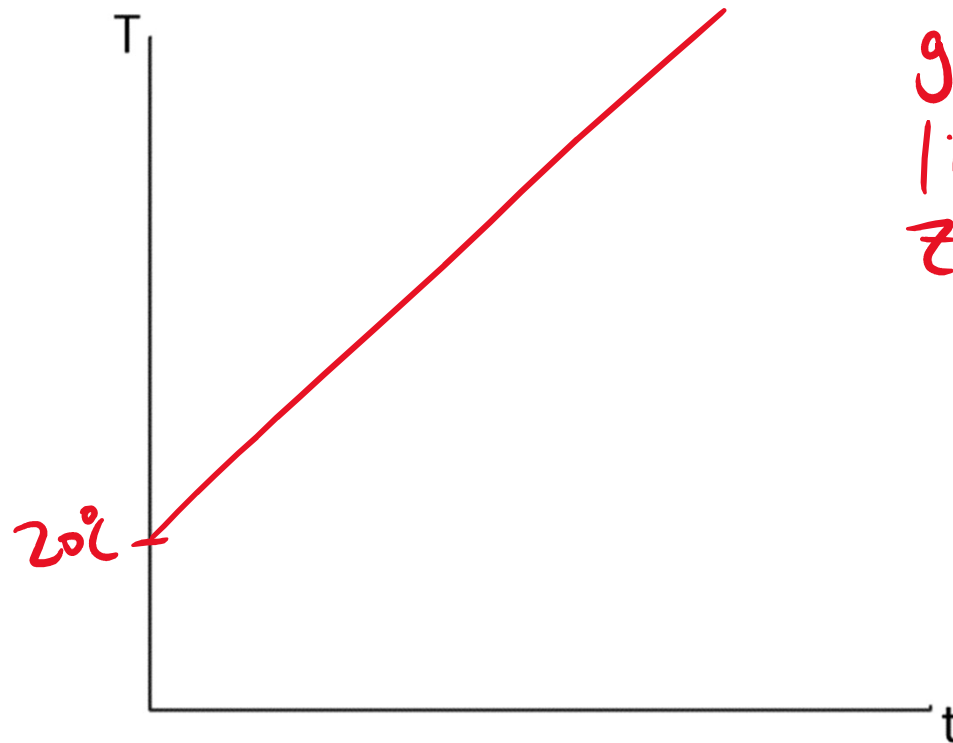
Sketch graphs (one for each block) showing how you expect the temperatures of the two blocks to behave as a function of time.

Sketch graphs (one for each block) showing how you expect the temperatures of the two blocks to behave as a function of time.





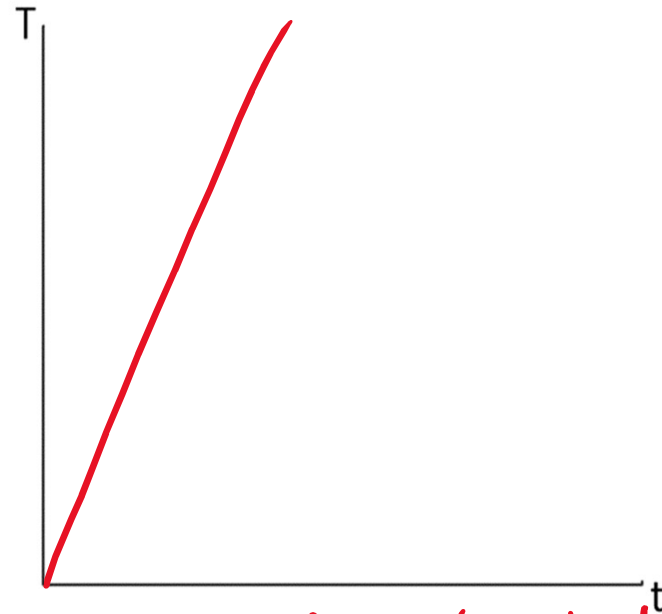
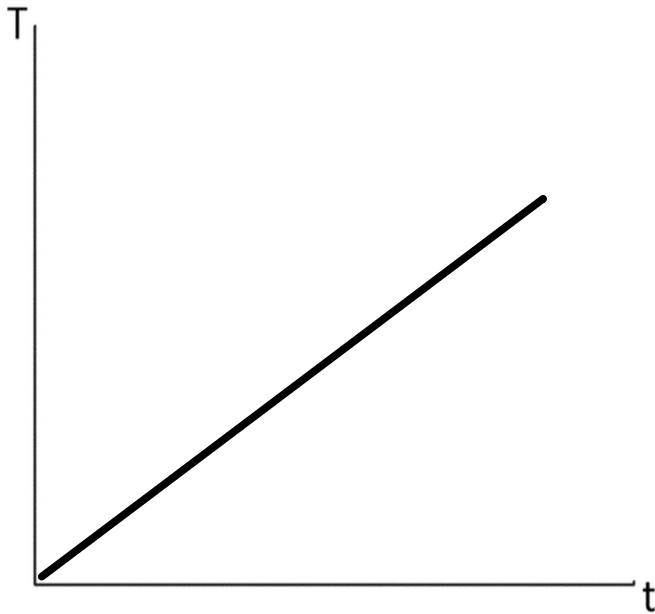
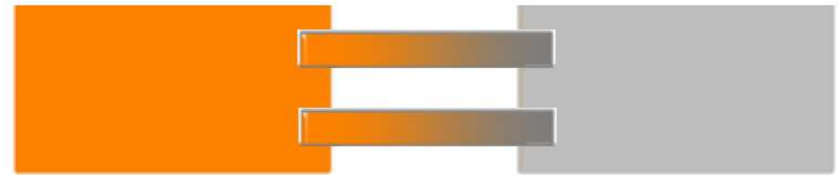
Sketch a graph of how the temperature behaves as a function of time at early times (remembering that the two blocks have already been connected for a while).



any smooth
graph looks
linear if we
zoom in enough



VS

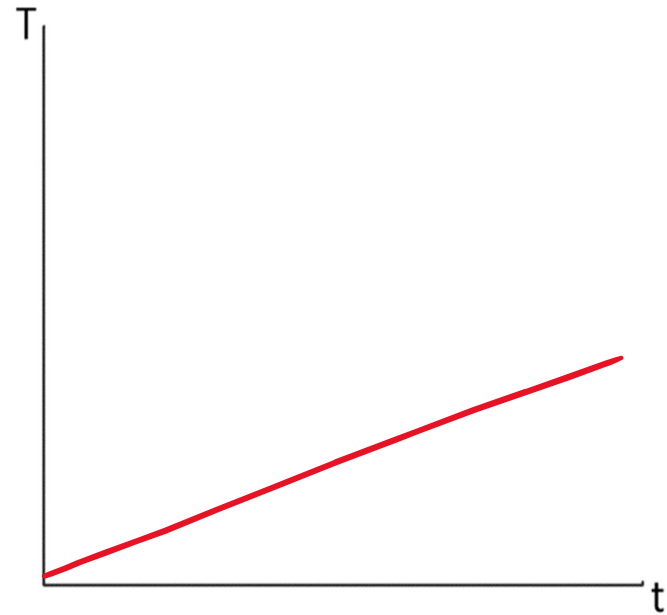
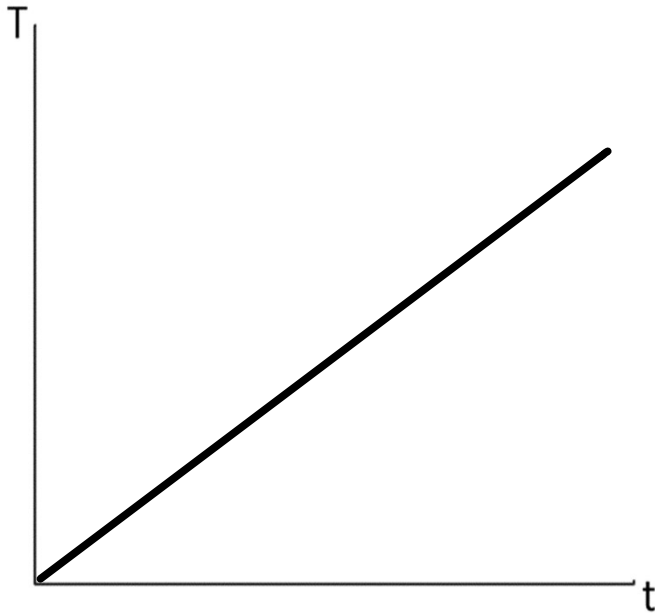


$$H = k A \frac{T_H - T_C}{L}$$

A is double here
so larger heat
current + faster
heating



VS

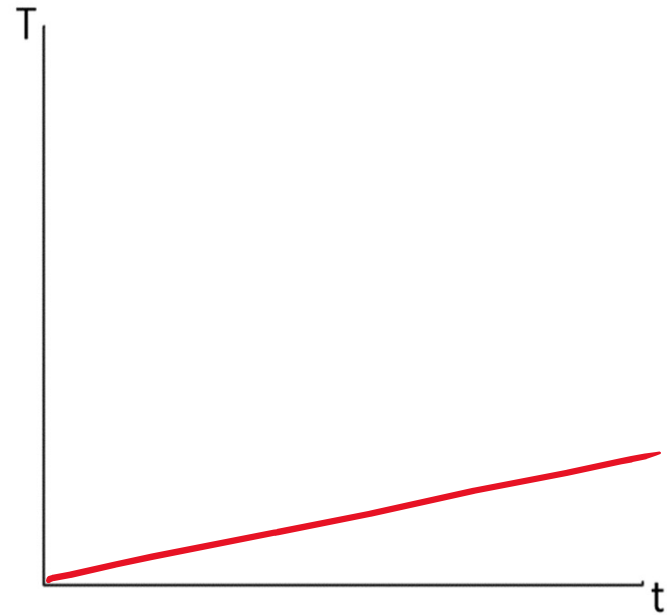
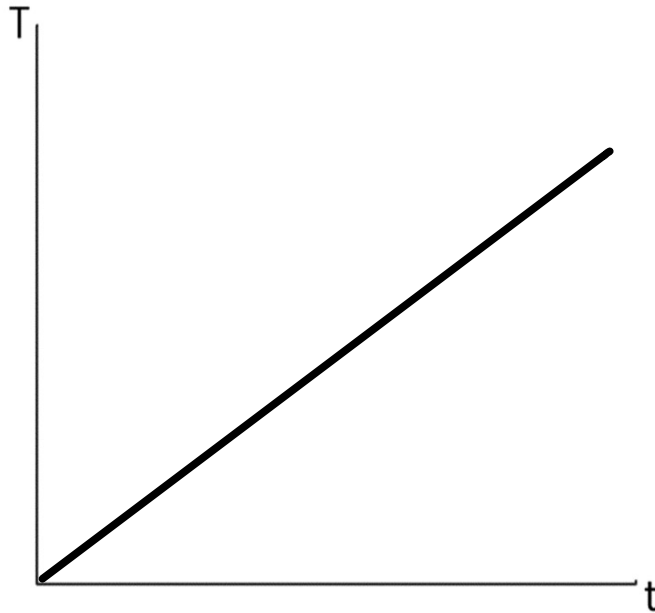
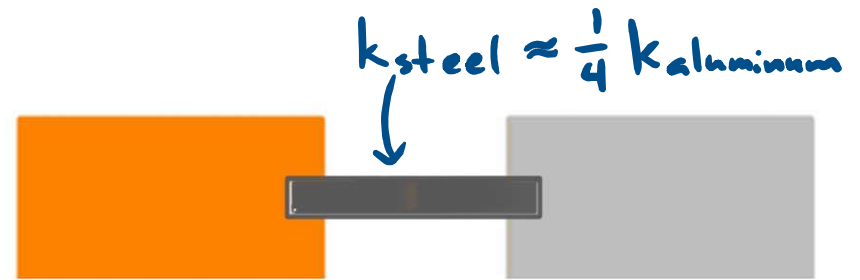


$$H = k A \frac{T_H - T_C}{L}$$

L is double
here so smaller
heat current and
slower heating



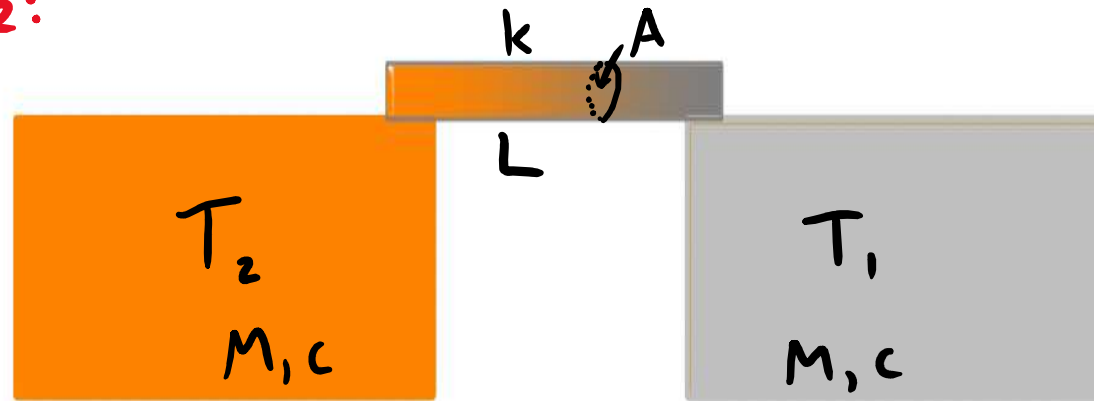
VS



$$H = k A \frac{T_H - T_C}{L}$$

k_s is $\frac{1}{4} k_{al}$. so
H will be 4x
smaller and
heating will be
slower

Next time:



What is the change in temperature dT of the cooler block that occurs in a small time dt ?

Hint: What is the meaning of H in the conductivity formula? In terms of H , how much heat is added to this block in the time dt ?

$$H = k A \frac{T_H - T_C}{L}$$

$$Q = M c \Delta T$$